

# An End-to-End DC-to-DC Efficiency Optimization and Design Analysis for MIMO Wireless Power Transfer Systems

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**Abstract**—This article presents an end-to-end DC-to-DC efficiency optimization framework for wireless power transfer (WPT) systems that jointly accounts for the nonlinear characteristics of both the power amplifier (PA) and the rectifier. Using measurement-based models—an affine function for the PA and a concave piecewise linear (PWL) function for the rectifier—the optimization is formulated as a semidefinite program (SDP) that directly maximizes the DC-to-DC efficiency under a transmit DC power budget constraint. When the SDP relaxation yields a higher rank solution that cannot be directly realized as a single beam, its objective value provides a reasonable upper bound on the achievable DC power; a successive convex approximation (SCA) procedure then recovers a feasible rank-one excitation vector, achieving a recovery ratio exceeding 97% across all tested conditions. Although the formulation is general and applicable to any array configuration, including SISO and MISO, it is validated on a multiple-input-multiple-output (MIMO) system where the near-field focusing effect is impactful. Three optimization frameworks—RF-to-RF, RF-to-DC, and DC-to-DC—are systematically compared. Simulation results using a 5.64-GHz system with a  $12 \times 12$  transmit array and an  $8 \times 8$  receive rectenna array show that the DC-to-DC optimization achieves 31% and 48% higher end-to-end efficiency than the RF-to-DC and RF-to-RF approaches, respectively, at a distance of 0.5 m. Experimental validation on a fabricated  $16 \times 16$  TX array and a  $5 \times 5$  rectenna confirms that the measured DC-to-DC efficiency closely follows the simulation across both distance and azimuth sweeps.

**Index Terms**—DC-to-DC efficiency, multiple-input-multiple-output (MIMO), rectenna, semidefinite programming, wireless power transfer (WPT).

## I. INTRODUCTION

WIRELESS power transfer (WPT) technology has been extensively studied over the past decades, motivated by the growing demand for cable-free power delivery to electronic devices [1], [2], [3], [4]. WPT can be broadly classified into three major categories. Inductive WPT has been successfully

commercialized in mobile devices under the Qi standard [5], [6]. Resonant WPT, demonstrated by Kurs et al. [7] through strongly coupled magnetic resonances, extends the effective range to mid-field distances and is being adopted in electric vehicle (EV) charging applications. RF-based WPT, pioneered by Brown [8] through microwave beam transmission experiments, can deliver power over the longest distances among the three categories by directly radiating electromagnetic energy [9]. Notably, this concept traces back to the original vision of Nikola Tesla, who first proposed the idea of wireless energy transfer [10].

However, compared with inductive and resonant WPT, RF-based WPT (hereafter referred to simply as WPT) suffers from inherently low system-level efficiency. In the propagation domain, the transmitted power spreads over distance, fundamentally limiting the energy captured by the receiver [14]. In the circuit domain, the power amplifier (PA) on the transmit side and the rectifier on the receive side each introduce nonlinear losses that further degrade the overall efficiency. These multistage losses together form a major bottleneck for practical WPT systems. Consequently, optimizing the *transmit excitation* at the transmitter array (TXA) to maximize the end-to-end efficiency is of critical importance.

Numerous studies have investigated WPT efficiency optimization in the RF domain. RF-to-RF efficiency, commonly referred to as power transfer efficiency (PTE) [15], [16] or beam collection efficiency (BCE) [17], [18], is hereinafter denoted as PTE in this article. Enhancing PTE has been studied through a variety of approaches [19], [20], [21], [22], [23], [24], [25], [26]. In the context of planar arrays, Oliveri et al. [19] formulated the PTE maximization as a generalized eigenvalue problem and obtained the optimal array weights in closed form. Zhang and Ho [27] further introduced a convex optimization framework for multiple-input-multiple-output (MIMO) systems, casting the energy beamforming problem as a semidefinite program (SDP) and showing that the optimal transmit covariance matrix admits a rank-one solution under a sum-(RF) power constraint. PTE has long served as a primary figure of merit (FoM) for characterizing WPT system performance due to its mathematical tractability and physical clarity. However, PTE alone cannot capture the behavior of the entire WPT system, as it entirely neglects the DC-domain losses introduced by the PA and rectifier.

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TABLE I  
COMPARISON OF END-TO-END WPT OPTIMIZATION FRAMEWORKS

| Ref.             | TX-RX         | Signal     | PA model                  | Rectifier model          | Optimization     | RX power      | Exp.       |
|------------------|---------------|------------|---------------------------|--------------------------|------------------|---------------|------------|
| [11]             | SISO          | Multi-tone | Rapp (analytical)         | Taylor 4th-order         | SCP + SQP        | $\mu\text{W}$ | No         |
| [12]             | MISO (DMA)    | Multi-tone | Linear                    | Taylor 4th-order         | AO + SCA         | $\mu\text{W}$ | No         |
| [13]             | MISO (hybrid) | Multi-tone | Rapp (analytical)         | Diode eq. (Lambert $W$ ) | PSO / DDPG       | $\mu\text{W}$ | No         |
| <b>This work</b> | <b>MIMO</b>   | <b>CW</b>  | <b>Meas.-based affine</b> | <b>Meas.-based PWL</b>   | <b>SDP + SCA</b> | <b>mW-W</b>   | <b>Yes</b> |

To address this limitation, several studies have explored RF-to-DC efficiency by incorporating the rectifier's nonlinear power conversion behavior. Wan and Huang [28] first introduced the concept of “transmission-conversion efficiency (TCE),” defined as the product of PTE and the rectifier's power conversion efficiency (PCE), and showed that optimizing the aperture magnitude distribution of the transmitting antenna can improve TCE compared with uniform excitation. Sun et al. [29] proposed an optimization strategy under nonuniform incident power density distribution, where the load resistance of each rectifier is individually optimized to maximize the total PCE of the rectenna array. However, these works addressed PTE and PCE improvements separately rather than jointly optimizing the transmit excitation vector to maximize TCE as a *unified metric*. Shen and Clerckx [30] took a step further by formulating a joint beamforming optimization that directly maximizes TCE. However, their rectifier model is based on a Taylor-series approximation of the diode current equation, which is only valid in the linear (small-signal) operating region and does not account for saturation effects at higher power levels. Subsequently, Lee et al. [31] proposed a TCE maximization framework that employs a measurement-based rectifier model, capturing the full nonlinear PCE characteristics including saturation. Despite these advances, all RF-to-DC approaches still do not account for PA nonlinearity on the transmit side.

In a practical WPT system, power is supplied in DC form at the transmitter and ultimately delivered as DC power to the load at the receiver. Therefore, DC-to-DC efficiency represents the major end-to-end FoM for WPT systems. Despite its importance, DC-to-DC efficiency has only recently been treated as an explicit optimization objective. Some earlier works computed the overall efficiency by simple stagewise multiplication: the product of PTE and PCE has been used to evaluate RF-to-DC efficiency [32], while DC-to-DC efficiency has been reported by further including the PA efficiency as an additional multiplicative factor [1], [33]. Jiang et al. [34] explicitly defined DC-to-DC efficiency as part of a system-level FoM and optimized it with respect to design parameters such as operating frequency and antenna aperture area, though their optimization target was cost-efficient system architecture rather than the transmit excitation vector.

More recently, end-to-end optimization frameworks that jointly account for PA and rectifier nonlinearities have emerged, primarily in the context of multitone waveform design. Zhang and Clerckx [11] addressed the fundamental tradeoff between PA and energy harvester nonlinearities, showing that high-PAPR waveforms favored by the rectifier conflict

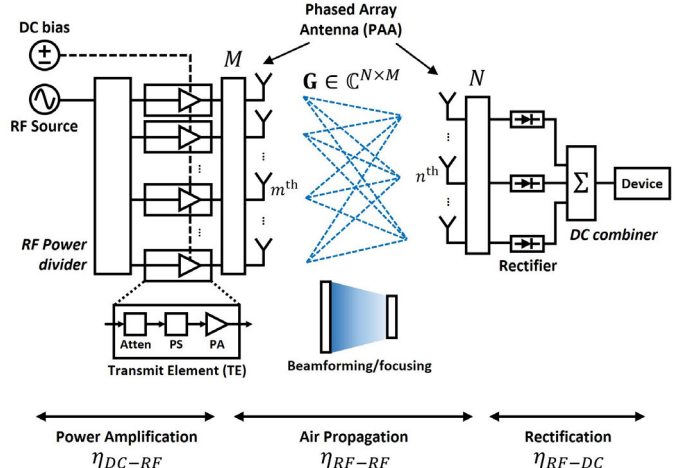


Fig. 1. Block diagram of the MIMO WPT system considered in this work. The end-to-end power flow consists of three stages: PA ( $\eta_{\text{DC-RF}}$ ), free-space channel ( $\eta_{\text{RF-RF}}$ ), and rectifier ( $\eta_{\text{RF-DC}}$ ).

with the PA's preference for low-PAPR signals; however, their formulation is restricted to a SISO link with an analytical Rapp PA model and a Taylor-expansion rectifier model. Azarbahram et al. [12] extended waveform optimization to a multi-antenna transmitter with dynamic metasurface antennas, but assumed linear PA operation and modeled only the rectifier nonlinearity. Khattak et al. [13], [35] proposed a joint waveform and hybrid beamforming design incorporating both the Rapp PA model and a diode-equation-based rectifier model; however, the solution was obtained through heuristic optimization, and the optimality gap was not explicitly quantified. As summarized in Table I, these works share several common characteristics: multitone waveform optimization in SISO or MISO configurations, analytical device models valid over a limited operating range, and no experimental validation. These aspects leave a gap for practical phased-array WPT systems, where continuous wave (CW) operation is practical, and the PA and rectifier behavior must be characterized across the full operating range.

This article addresses this gap by proposing a *DC-to-DC efficiency optimization framework for practical CW-based MIMO WPT systems* that encompasses all three power conversion stages: PA, free-space propagation channel, and rectifier. The proposed framework targets a different design domain from the multitone waveform approaches in [11], [12], and [13]: it directly optimizes the CW excitation vector of a phased-array transmitter, which is the prevailing architecture in practical WPT deployments. Rather than relying on analytical

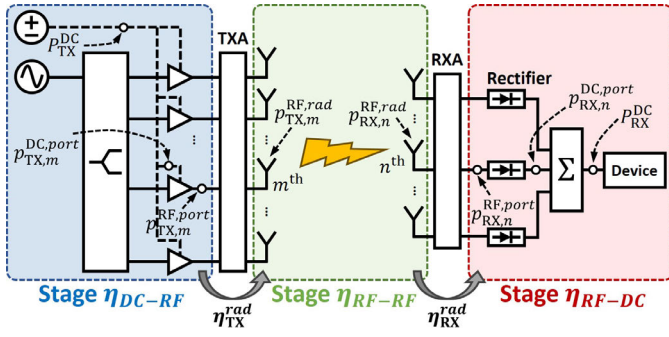


Fig. 2. Detailed power flow and per-element variables across the three stages. Superscripts “port” and “rad” distinguish antenna port-level and radiated quantities, respectively. Lowercase variables ( $p$ ) denote per-element quantities, and uppercase variables ( $P$ ) denote system-level totals.

device equations, the PA and rectifier behaviors are captured through measurement-based piecewise linear (PWL) models derived from hardware characterization, enabling accurate representation of device behavior across the full operating range, including saturation. The resulting optimization is cast as an SDP via SDR [36], and a successive convex approximation (SCA) procedure [37] is developed to recover a feasible rank-one excitation vector from the relaxed solution. By providing both an efficiency upper bound and a feasible excitation vector for any given hardware configuration, this framework serves as a practical tool for RF engineers to evaluate achievable system-level performance and to determine the optimal transmit excitation for maximum DC power delivery. The main contributions are as follows.

- 1) A DC-to-DC optimization framework for MIMO WPT systems that jointly accounts for PA and rectifier nonlinearities through measurement-based models capturing the device characteristics across the operating range.
- 2) An SDP-based formulation that provides both an upper bound on the achievable DC-to-DC efficiency for a given system configuration and a high-quality feasible excitation through SCA-based rank-one recovery.
- 3) A systematic comparative analysis of three optimization strategies—RF-to-RF (PTE), RF-to-DC (TCE), and DC-to-DC—under consistent conditions across diverse scenarios, quantifying how PA and rectifier nonlinear coupling affects the optimal excitation design.
- 4) Experimental validation using a TXA and rectenna prototype, demonstrating the accuracy of the DC-to-DC framework under real-world operating conditions.

The TXA hardware used in this work was fabricated and calibrated in our prior work [38], [39], [40]. Preliminary results of this study were first presented in [41].

The remainder of this article is organized as follows. Section II describes the MIMO WPT system model and defines the efficiency metrics. Section III presents the three optimization frameworks: RF-to-RF (PTE), RF-to-DC (TCE), and the proposed DC-to-DC, along with the SCA-based rank-one recovery procedure. Section IV provides simulation results and comparative analysis across multiple scenarios. Section V presents experimental validation through measurements. Section VI discusses the modeling scope and

projects the performance with state-of-the-art devices. Finally, Section VII concludes this article.

## II. BACKGROUND

### A. System Model

Fig. 1 illustrates the MIMO WPT system considered in this work. The transmitter side consists of a TXA with  $M$  antenna elements. A common RF source feeds all transmit paths via a power divider, and each path forms a transmit element (TE) comprising an attenuator, a phase shifter (PS), and a PA in cascade, enabling independent control of the magnitude and phase at each element.<sup>1</sup> The receiver side consists of a receiver array (RXA) with  $N$  rectifying elements, where each element rectifies the incoming RF power independently. The DC outputs from all rectifiers are then combined through a DC combiner to deliver the total DC power to the load.

The end-to-end power flow from the DC supply to the load traverses three distinct stages, as indicated in Fig. 1.

- 1) *Power Amplification Stage* ( $\eta_{DC-RF}$ ): Each PA consumes DC power to amplify the RF signal. Due to the nonlinear input-output characteristics of practical PAs, the efficiency varies with the operating power level.
- 2) *Air Propagation Stage* ( $\eta_{RF-RF}$ ): The RF signals radiated by the TXA propagate through free space and are captured by the RXA. The received power at each RXA element depends on the transmit excitation, the array geometry, and the propagation environment.
- 3) *Rectification Stage* ( $\eta_{RF-DC}$ ): Each rectifier converts the received RF power into DC power. Like the PA, the rectifier exhibits nonlinear conversion characteristics that depend on the input power level.

The following assumptions are adopted across this article.

- 1) Free-space propagation is assumed for the channel.
- 2) All PAs and all rectifiers are assumed to have identical nonlinear characteristics, modeled based on measurement data as detailed in Section III.
- 3) DC power combining at the RXA is ideal, i.e., the total received DC power equals the arithmetic sum of the individual rectifier outputs.<sup>2</sup>

### B. System Efficiency Metrics

Throughout this article, the three system-level efficiencies are referred to as “RF-to-RF,” “RF-to-DC,” and “DC-to-DC.” For brevity, these terms are abbreviated as “RF-RF,” “RF-DC,” and “DC-DC,” respectively, in this article title, figure captions, table entries, and subscripts.

Figs. 2 and 3 detail the power flow variables and efficiency metric definitions at each stage. At the transmitter, the  $m$ th PA consumes DC power  $p_{TX,m}^{DC,port}$  and delivers RF output power

<sup>1</sup>Most of the WPT systems omit the attenuator and transmit at full power with phase-only control to reduce hardware complexity, and also to achieve higher power at the receiver. The architecture shown here represents the general case where both magnitude and phase are adjustable, since magnitude tapering significantly affects the system efficiency.

<sup>2</sup>The design of practical DC combining or mathematical modeling of the combining framework is beyond the scope of this article.

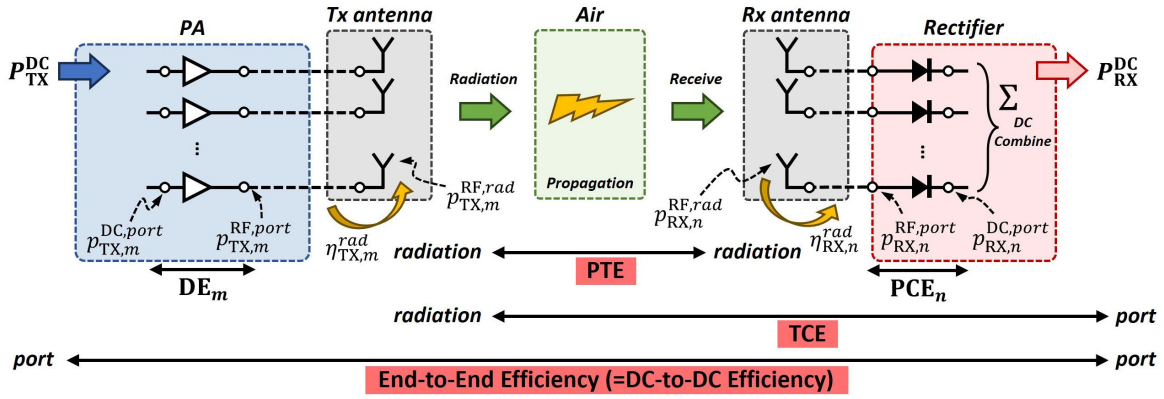


Fig. 3. System-level power flow and efficiency metric definitions.  $DE_m$ , PTE,  $PCE_n$ , TCE, and end-to-end efficiency span progressively broader portions of the power chain. The radiation efficiencies  $\eta_{TX,m}^{\text{rad}}$  and  $\eta_{RX,n}^{\text{rad}}$  bridge the port-level and radiated quantities.

$p_{TX,m}^{\text{RF, port}}$  at the antenna port. The drain efficiency (DE) of the  $m$ th PA is defined as

$$DE_m = \frac{p_{TX,m}^{\text{RF, port}}}{p_{TX,m}^{\text{DC, port}}} \quad (1)$$

At the receiver, the  $n$ th rectifier receives RF power  $p_{RX,n}^{\text{RF, port}}$  at its input port and produces DC output power  $p_{RX,n}^{\text{DC, port}}$ . The PCE of the  $n$ th rectifier is

$$PCE_n = \frac{p_{RX,n}^{\text{DC, port}}}{p_{RX,n}^{\text{RF, port}}} \quad (2)$$

The system-level power quantities are obtained by summing over all elements

$$P_{TX}^{\text{DC}} = \sum_{m=1}^M p_{TX,m}^{\text{DC, port}}, \quad P_{TX}^{\text{RF, port}} = \sum_{m=1}^M p_{TX,m}^{\text{RF, port}} \quad (3)$$

$$P_{RX}^{\text{RF, port}} = \sum_{n=1}^N p_{RX,n}^{\text{RF, port}}, \quad P_{RX}^{\text{DC}} = \sum_{n=1}^N p_{RX,n}^{\text{DC, port}} \quad (4)$$

where  $P_{TX}^{\text{RF, port}}$  and  $P_{RX}^{\text{RF, port}}$  denote the total RF power at the transmit and receive antenna ports, respectively.

The end-to-end DC-to-DC efficiency is defined as

$$\eta_{\text{DC-DC}} = \frac{P_{RX}^{\text{DC}}}{P_{TX}^{\text{DC}}} \quad (5)$$

To decompose  $\eta_{\text{DC-DC}}$  into physically meaningful stages, the antenna radiation efficiency must be accounted for, as indicated in Fig. 2. Let  $\eta_{TX,m}^{\text{rad}}$  and  $\eta_{RX,n}^{\text{rad}}$  be the radiation efficiency of the  $m$ th transmit and  $n$ th receive antenna element, respectively. The per-element radiated power from the  $m$ th transmit antenna and the per-element power incident on the  $n$ th receive antenna (before the antenna loss) are

$$p_{TX,m}^{\text{RF, rad}} = \eta_{TX,m}^{\text{rad}} \cdot p_{TX,m}^{\text{RF, port}}, \quad p_{RX,n}^{\text{RF, rad}} = \frac{p_{RX,n}^{\text{RF, port}}}{\eta_{RX,n}^{\text{rad}}} \quad (6)$$

and the corresponding system-level totals are

$$P_{TX}^{\text{RF, rad}} = \sum_{m=1}^M \eta_{TX,m}^{\text{rad}} \cdot p_{TX,m}^{\text{RF, port}} \quad (7)$$

$$P_{RX}^{\text{RF, rad}} = \sum_{n=1}^N \frac{p_{RX,n}^{\text{RF, port}}}{\eta_{RX,n}^{\text{rad}}} \quad (8)$$

PTE is then defined as the radiated-to-radiated efficiency

$$\eta_{\text{RF-RF}} \text{ (PTE)} = \frac{P_{RX}^{\text{RF, rad}}}{P_{TX}^{\text{RF, rad}}} \quad (9)$$

which is equivalent to the BCE defined in [18], [19], and [40], quantifying the fraction of total radiated power collected at the receiver aperture.

Using these definitions, the end-to-end efficiency is expressed as  $\eta_{\text{DC-DC}} = P_{RX}^{\text{DC}}/P_{TX}^{\text{DC}}$ , where  $\eta_{\text{DC-RF}} = P_{TX}^{\text{RF, port}}/P_{TX}^{\text{DC}}$  is the system-level PA efficiency and  $\eta_{\text{RF-DC}} = P_{RX}^{\text{DC}}/P_{RX}^{\text{RF, port}}$  is the system-level rectifier efficiency, as labeled in Fig. 2. When all antenna elements are identical, i.e.,  $\eta_{TX,m}^{\text{rad}} = \eta_{TX}^{\text{rad}}$  for all  $m$  and  $\eta_{RX,n}^{\text{rad}} = \eta_{RX}^{\text{rad}}$  for all  $n$ , this simplifies to the cascade form

$$\eta_{\text{DC-DC}} = \underbrace{\eta_{\text{DC-RF}}}_{\text{PA}} \cdot \underbrace{\eta_{\text{RF-RF}}}_{\text{Air propagation}} \cdot \underbrace{\eta_{\text{RF-DC}}}_{\text{Rectifier}} \quad (10)$$

where  $\eta_{TX}^{\text{rad}}$  and  $\eta_{RX}^{\text{rad}}$  become fixed constants independent of the excitation, whereas the three stage efficiencies  $\eta_{\text{DC-RF}}$ ,  $\eta_{\text{RF-RF}}$ , and  $\eta_{\text{RF-DC}}$  vary with the operating conditions.

While (10) provides a clean decomposition, optimizing each stage independently is suboptimal due to the nonlinear coupling between them. The PA excitation determines the transmit beam pattern, governing PTE, and simultaneously shapes the received power distribution across the rectifier array, governing the per-element PCE. This interstage coupling motivates the direct optimization of  $\eta_{\text{DC-DC}}$  formulated in Section III.

### III. OPTIMIZATION FRAMEWORKS

This section formulates three optimization problems that correspond to progressively more comprehensive efficiency metrics: RF-to-RF (PTE), RF-to-DC (TCE), and DC-to-DC. Throughout this section, all antenna elements are assumed to be identical, so that  $\eta_{TX,m}^{\text{rad}} = \eta_{TX}^{\text{rad}}$  for all  $m$  and  $\eta_{RX,n}^{\text{rad}} = \eta_{RX}^{\text{rad}}$  for all  $n$ . Since these radiation efficiencies are then fixed constants independent of the transmit excitation, they do not influence the optimal solution and are omitted from the optimization formulations hereafter.

### A. System Architecture and Channel Model

Let  $G \in \mathbb{C}^{N \times M}$  be the channel matrix between the TXA and RXA, and let  $x_t \in \mathbb{C}^{M \times 1}$  be the transmit excitation vector. The channel matrix  $G$  is computed from the free-space propagation model incorporating the antenna element patterns. The transmit covariance matrix is defined as  $S = \mathbb{E}[x_t x_t^H] \geq 0$ . Using  $S$ , the per-element transmit and receive RF powers at the antenna ports are expressed as

$$p_{TX,m}(S) = S_{mm}/Z \quad (11)$$

$$p_{RX,n}(S) = \text{tr}(C_n S)/Z \quad (12)$$

where  $Z$  is the characteristic impedance and  $C_n = G^H E_n G$ , with  $E_n \in \mathbb{R}^{N \times N}$  being the selection matrix whose only nonzero entry is  $[E_n]_{nn} = 1$ .

The rectifier and PA behaviors are modeled by measurement-based functions. The rectifier maps RF input power to DC output power through a concave PWL

$$p_{RX,n}^{\text{DC,port}} = f(p_{RX,n}^{\text{RF,port}}) = \min_{k \in \mathcal{K}} (a_k p_{RX,n}^{\text{RF,port}} + b_k) \quad (13)$$

where  $\{(a_k, b_k)\}_{k \in \mathcal{K}}$  are the slopes and intercepts of the  $|\mathcal{K}|$  segments. The concavity of  $f(\cdot)$  reflects the decreasing PCE at high input power due to rectifier saturation. The PA maps RF output power to the DC consumption through an affine function

$$p_{TX,m}^{\text{DC,port}} = h(p_{TX,m}^{\text{RF,port}}) = \alpha p_{TX,m}^{\text{RF,port}} + \beta \quad (14)$$

where  $\alpha$  and  $\beta$  are the slope and intercept obtained from measurement-based regression. Under the identical-element assumption, the same  $f(\cdot)$  and  $h(\cdot)$  apply to all rectifiers and PAs, respectively.

### B. RF-to-RF Efficiency (PTE) Optimization

The PTE optimization maximizes the total received RF power for a given total transmit RF power. Since maximizing  $p_{RX}^{\text{RF,rad}}$  under fixed  $p_{TX}^{\text{RF,rad}}$  is equivalent to maximizing  $\eta_{\text{RF-RF}}$  (PTE), the problem is formulated as [40]

$$\max_S \text{tr}(G S G^H)/Z \quad (15a)$$

$$\text{s.t. } \text{tr}(S)/Z = p_t^{\text{RF}} \quad (15b)$$

$$S \geq 0 \quad (15c)$$

where  $p_t^{\text{RF}}$  is the total transmit RF power budget. The objective is linear in  $S$ , making this a standard SDP with a globally optimal solution. The rank of the optimal  $S^*$  is guaranteed to be one for this formulation, and the optimal transmit vector is directly obtained as  $x_t^* = (\lambda_1)^{1/2} v_1$  from the eigenvalue decomposition of  $S^*$ .

Equivalently, the PTE maximization also can be expressed as the Rayleigh quotient [19]:<sup>3</sup>

$$\eta_{\text{RF-RF}} = \frac{x_t^H G^H G x_t}{x_t^H x_t} \quad (16)$$

<sup>3</sup>Since the channel matrix  $G$  is constructed from the realized gain, which embeds the antenna radiation efficiency, the ratio in (16) corresponds to the port-to-port power ratio rather than the radiated-to-radiated PTE. However, the two differ only by the constant factor  $\eta_{\text{TX}}^{\text{rad}} \cdot \eta_{\text{RX}}^{\text{rad}}$ , so the optimal excitation vector is identical.

whose maximum is attained by the dominant eigenvector of  $G^H G$ . This generalized eigenvalue formulation admits a closed-form solution and guarantees global optimality. The absence of PA and rectifier constraints makes this closed-form solution possible. When such nonlinear device constraints are introduced—as in the TCE and DC-to-DC formulations below—the problem no longer reduces to an eigenvalue problem, and finding the globally optimal excitation vector directly becomes intractable.

### C. RF-to-DC Efficiency (TCE) Optimization

TCE optimization extends the scope of PTE optimization to include the rectifier behavior [31]. By incorporating the concave PWL rectifier model (13) into the PTE formulation, the problem becomes:<sup>4</sup>

$$\max_{S,t} \sum_{n=1}^N t_n \quad (17a)$$

$$\text{s.t. } \text{tr}(S)/Z \leq p_t^{\text{RF}} \quad (17b)$$

$$S \geq 0 \quad (17c)$$

$$t_n \leq a_k p_{RX,n}(S) + b_k \quad \forall n \quad \forall k \in \mathcal{K} \quad (17d)$$

$$p_{RX,n}^{\min} \leq p_{RX,n}(S) \leq p_{RX,n}^{\max} \quad \forall n \quad (17e)$$

where  $t_n$  is an auxiliary variable representing the DC output of the  $n$ th rectifier, upper bounded by the PWL approximation of  $f(\cdot)$  through the hypograph constraints. The input power range  $[p_{RX,n}^{\min}, p_{RX,n}^{\max}]$  enforces valid rectifier operating conditions. Since  $f(\cdot)$  is concave, the hypograph constraints are linear in  $S$  and  $t$ , preserving the SDP structure. Note that the power constraint (17b) uses an inequality rather than the equality in (15b): unlike PTE, where using the full power budget is always optimal, the TCE optimizer may benefit from transmitting less than  $p_t^{\text{RF}}$  to avoid driving rectifiers into saturation.

### D. DC-to-DC Efficiency Optimization

1) *Problem Formulation:* The DC-to-DC formulation incorporates both the PA and rectifier nonlinearities, jointly optimizing the transmit excitation under a DC power budget

$$\max_{S,t} \sum_{n=1}^N t_n \quad (18a)$$

$$\text{s.t. } \frac{\alpha}{Z} \text{tr}(S) + M\beta \leq p_t^{\text{DC}} \quad (18b)$$

$$S \geq 0 \quad (18c)$$

$$t_n \leq a_k p_{RX,n}(S) + b_k \quad \forall n \quad \forall k \in \mathcal{K} \quad (18d)$$

$$p_{RX,n}^{\min} \leq p_{RX,n}(S) \leq p_{RX,n}^{\max} \quad \forall n \quad (18e)$$

$$p_{TX,m}^{\min} \leq p_{TX,m}(S) \leq p_{TX,m}^{\max} \quad \forall m \quad (18f)$$

<sup>4</sup>In [31], TCE optimization was solved via mixed-integer nonlinear programming (MINLP) to handle a general piecewise rectifier model. Since the rectifier model adopted in this article is restricted to concave PWL segments, the problem can be reformulated as an SDP with equivalent results. The additional rectifier constraints, however, do not guarantee a rank-one  $S^*$ ; when the rank exceeds one, the same SCA-based rank-one recovery in Section III-D is applied. In practice, the rank remains low (typically  $\leq 2$ ).

where  $P_t^{\text{DC}}$  is the total DC power budget. The output power range  $[p_{\text{TX},m}^{\min}, p_{\text{TX},m}^{\max}]$  enforces the valid RF output-power operating range of  $m$ th PA. The key difference from the TCE formulation (17) is the incorporation of the PA characteristic: the power budget is imposed on the  $P_t^{\text{DC}}$  rather than on the RF output. Since  $h(\cdot)$  is affine, the total PA DC consumption  $\sum_{m=1}^M h(p_{\text{TX},m}) = (\alpha/Z)\text{tr}(S) + M\beta$  reduces to a single linear constraint on  $\mathbf{S}$ , preserving the SDP structure without requiring auxiliary variables.

Since all constraints are linear in  $\mathbf{S}$  and  $\mathbf{t}$ , this formulation is an SDP that can be solved globally using standard convex optimization tools. The globally optimal  $S^*$  may have rank greater than one and therefore does not directly correspond to a single transmit excitation vector. Nevertheless, its objective value  $\bar{P}_{\text{DC}} = \sum_{n=1}^N t_n^*$  represents the maximum total received DC power under the relaxed-rank constraint, providing an upper bound that no feasible single-beam solution can exceed.

2) *Rank-One Recovery via SCA*: Since a practical CW transmitter requires a single excitation vector  $x_t$ , a rank-one solution must be recovered from  $S^*$  when its rank exceeds one. The upper bound  $\bar{P}_{\text{DC}}$  established above certifies the quality of any recovered solution:  $\sum_{n=1}^N f(p_{\text{RX},n}(x_t)) \leq \bar{P}_{\text{DC}}$  for all feasible  $x_t$ .

A rank- $r$  solution  $S^* = \sum_{i=1}^r \lambda_i v_i v_i^H$  can be interpreted as a time-sharing of  $r$  beams, where each eigenmode  $v_i$  would be transmitted for a fraction of time proportional to  $\lambda_i$ . These eigenmodes are jointly optimal under this relaxed-rank (time-division) assumption, but they do not necessarily span the best single-beam solution. Restricting the search to  $x_t = \sum_{i=1}^K c_i v_i$  confines the optimization to a  $K$ -dimensional subspace of  $\mathbb{C}^M$  dictated by the time-division-optimal modes, potentially missing single-beam solutions that better exploit the hardware constraints. Since the optimal single-beam excitation is not guaranteed to lie in this subspace, we formulate the rank-one recovery as a direct optimization over the full  $\mathbb{C}^M$  space using SCA [37].

The rank-one problem is stated as

$$\max_{x_t \in \mathbb{C}^M} \sum_{n=1}^N f(p_{\text{RX},n}(x_t)) \quad (19a)$$

$$\text{s.t. } p_{\text{TX},m}^{\min} \leq p_{\text{TX},m}(x_t) \leq p_{\text{TX},m}^{\max} \quad \forall m \quad (19b)$$

$$0 \leq p_{\text{RX},n}(x_t) \leq p_{\text{RX},n}^{\max} \quad \forall n \quad (19c)$$

$$\frac{\alpha}{Z} \|x_t\|^2 + M\beta \leq P_t^{\text{DC}} \quad (19d)$$

where  $p_{\text{TX},m}(x_t) = |x_{t,m}|^2/Z$  and  $p_{\text{RX},n}(x_t) = |g_n^H x_t|^2/Z$ , with  $g_n^H$  denoting the  $n$ th row of  $\mathbf{G}$ . This problem is nonconvex because the objective involves a concave function  $f(\cdot)$ , composed with the convex quadratic  $|g_n^H x_t|^2/Z$ .

SCA resolves this nonconvexity by replacing the convex quadratic terms with affine lower bounds at each iteration. At the  $i$ th iteration with current point  $x_t^{(i)}$ , the received power  $p_{\text{RX},n}(x_t)$  is replaced by its first-order affine minorizer

$$\hat{q}_n(x_t; x_t^{(i)}) = \frac{2}{Z} \text{Re} \left( (g_n^H x_t^{(i)})^* g_n^H x_t \right) - \frac{|g_n^H x_t^{(i)}|^2}{Z} \quad (20)$$

which satisfies two properties: tangent point agreement,  $\hat{q}_n(x_t^{(i)}; x_t^{(i)}) = p_{\text{RX},n}(x_t^{(i)})$ , and global lower bound,  $\hat{q}_n(x_t; x_t^{(i)}) \leq$

### Algorithm 1 SCA-SOCP Rank-One Recovery

**Require:** SDP solution  $S^*$ , upper bound  $\bar{P}_{\text{DC}}$ , tolerance  $\varepsilon$

**Ensure:** Feasible transmit vector  $\mathbf{x}_t^*$ , recovery ratio  $\rho_{\text{rec}}$

```

1: Compute EVD:  $\mathbf{S}^* = \sum_i \lambda_i \mathbf{v}_i \mathbf{v}_i^H$ ,  $\lambda_1 \geq \lambda_2 \geq \dots$ 
2: Initialize  $\mathbf{x}_t^{(0)} \leftarrow \gamma \sqrt{\lambda_1} \mathbf{v}_1$  (warm start)  $\triangleright \gamma$ : feasibility scaling
3: for  $i = 0, 1, 2, \dots$  do
4:   Compute  $\hat{q}_n(\cdot; \mathbf{x}_t^{(i)})$  for all  $n$  via (20)
5:   Solve SOCP (21)  $\rightarrow \mathbf{x}_t^{(i+1)}$ 
6:   Evaluate  $F(\mathbf{x}_t^{(i+1)}) = \sum_n \max(f(p_{\text{RX},n}(\mathbf{x}_t^{(i+1)}), 0)$ 
7:   if  $|F(\mathbf{x}_t^{(i+1)}) - F(\mathbf{x}_t^{(i)})| < \varepsilon$  then
8:     break
9:   end if
10: end for
11:  $\mathbf{x}_t^* \leftarrow \mathbf{x}_t^{(i+1)}$ 
12:  $\rho_{\text{rec}} \leftarrow F(\mathbf{x}_t^*)/\bar{P}_{\text{DC}}$ 
13: return  $\mathbf{x}_t^*, \rho_{\text{rec}}$ 
```

$p_{\text{RX},n}(x_t)$  for all  $x_t$ . The derivation from the first-order convexity condition is provided in Appendix A. Since  $f(\cdot)$  is concave and nondecreasing over the valid input range, and  $\hat{q}_n$  is affine in  $x_t$ , the surrogate objective  $\tilde{F}(x_t; x_t^{(i)}) = \sum_{n=1}^N f(\hat{q}_n(x_t; x_t^{(i)}))$  is concave. Maximizing this surrogate at each iteration yields the following second-order cone program (SOCP) subproblem:

$$\max_{x_t, t} \sum_{n=1}^N t_n \quad (21a)$$

$$\text{s.t. } t_n \leq a_k \hat{q}_n(x_t; x_t^{(i)}) + b_k \quad \forall n \quad \forall k \in \mathcal{K} \quad (21b)$$

$$\hat{q}_n(x_t; x_t^{(i)}) \geq 0 \quad \forall n \quad (21c)$$

$$|g_n^H x_t| \leq \sqrt{p_{\text{RX},n}^{\max} \cdot Z} \quad \forall n \quad (21d)$$

$$|x_{t,m}| \leq \sqrt{p_{\text{TX},m}^{\max} \cdot Z} \quad \forall m \quad (21e)$$

$$\frac{\alpha}{Z} \|x_t\|^2 + M\beta \leq P_t^{\text{DC}}. \quad (21f)$$

The first two sets of constraints are linear in  $x_t$  (since  $\hat{q}_n$  is affine), while the remaining three are SOC constraints, confirming the SOCP structure. This subproblem is convex and can be solved to global optimality at each SCA iteration. In deriving (21), the lower PA output-power constraint  $p_{\text{TX},m}^{\min} \leq p_{\text{TX},m}(x_t)$  in (19b) is relaxed because it is nonconvex in  $x_t$ , whereas the upper PA output-power constraint is convex and retained as (21e).

The SCA iterates  $\{x_t^{(i)}\}$  produce a monotonically nondecreasing sequence of objective values, i.e.,  $F(x_t^{(i+1)}) \geq F(x_t^{(i)})$ , where  $F(x_t) = \sum_{n=1}^N f(p_{\text{RX},n}(x_t))$ . Since this sequence is bounded above by  $\bar{P}_{\text{DC}}$ , convergence to a KKT stationary point of (19) is guaranteed (proof in Appendix B).

The SDP solution plays a dual role in this procedure: it provides the upper bound  $\bar{P}_{\text{DC}}$  for quality certification, and its dominant eigenvector  $(\lambda_1)^{1/2} \mathbf{v}_1$ —scaled to satisfy the feasibility constraints—serves as a warm start for the SCA iterations, initiating the search from a direction that the relaxed optimization has already identified as favorable.

The quality of the recovered solution is measured by the new metric defined as the *recovery ratio*

$$\rho_{\text{rec}} = \frac{P_{\text{DC}}^*}{\bar{P}_{\text{DC}}} \quad (22)$$

where  $P_{DC}^* = \sum_{n=1}^N \max(f(p_{RX,n}(x_t^*)), 0)$  is the total received DC power achieved by the final solution  $x_t^*$ , and the  $\max(\cdot, 0)$  operator clamps the PWL model output to zero, since  $f(\cdot)$  may return negative values at very low input powers as an artifact of the regression. A recovery ratio close to unity indicates that the SDP relaxation is tight and the recovered single-beam solution is near-optimal. The overall procedure is summarized in Algorithm 1.

#### IV. SIMULATION RESULTS AND DESIGN ANALYSIS

##### A. Simulation Setup

All simulations are performed in MATLAB on a desktop PC with an AMD Ryzen 7 5800X processor. The channel matrix  $\mathbf{G}$  defined in Section III-A is constructed from the Friis free-space propagation model. The  $(n, m)$ th entry of  $\mathbf{G} \in \mathbb{C}^{N \times M}$ , representing the channel from the  $m$ th TXA element to the  $n$ th RXA element, is expressed on a voltage scale as

$$G_{n,m} = |G_{n,m}| e^{j\angle G_{n,m}} \quad (23)$$

with the magnitude and phase given by

$$|G_{n,m}| = \frac{\lambda}{4\pi d_{n,m}} \sqrt{G_{TX}(\theta_{TX,n,m}) G_{RX}(\theta_{RX,n,m})} \quad (24)$$

$$\angle G_{n,m} = \frac{2\pi}{\lambda} \cdot d_{n,m} = k \cdot d_{n,m} \quad (25)$$

where  $d_{n,m}$  is the distance between the  $m$ th TXA element and the  $n$ th RXA element,  $G_{TX}(\theta)$  and  $G_{RX}(\theta)$  are the identical active element gain patterns of the TXA and RXA, respectively, and  $\lambda$  is the operating wavelength. The antenna radiation efficiency was  $\eta_{\text{rad}} = 86\%$ . The antenna element design and characterization are detailed in [40]. Both the TXA and RXA are planar square arrays<sup>5</sup> ( $M_t \times M_t$  and  $N_r \times N_r$ , respectively), where  $M_t$  and  $N_r$  are the number of elements along one side of each square array, with element spacing  $0.6\lambda$  at the operating frequency of 5.64 GHz,<sup>6</sup> and  $Z = 50 \Omega$ .

The rectifier and PA characteristics are captured by the measurement-based functions  $f(\cdot)$  and  $h(\cdot)$  defined in (13) and (14), respectively, and the same functions are used consistently throughout both the simulation analysis and experimental validation. The SDP problems (15)–(18) are solved using the CVX toolbox with the MOSEK solver for the RF–RF and DC–DC formulations and the SeDuMi solver for the RF–DC formulation. The SCA-SOCP rank-one recovery (Algorithm 1) is initialized with the dominant eigenvector of  $S^*$  and uses a convergence tolerance of  $\varepsilon = 10^{-4}$ .

The PA model  $h(\cdot)$  is derived from measurements of the Skyworks SE5004L [42], a 5-GHz PA with a typical 1-dB compression point of 30–34 dBm. The same PA chip is used in the TXA TEs; however, since the on-board PA is not individually accessible for direct measurement, the characterization is performed using the manufacturer's evaluation board (SE5004L-EK1 EVB) [43], shown in Fig. 4. The EVB

<sup>5</sup>A square array is assumed only for simplicity. The framework itself is geometry-agnostic and applies to any (e.g., rectangular or nonuniform) array, as it depends solely on the resulting channel matrix  $\mathbf{G}$ .

<sup>6</sup>The operating frequency of 5.64 GHz was selected based on the measured array-level response of the fabricated  $16 \times 16$  TXA [40], whose best matching response occurred near 5.64 GHz after full RF-chain integration.

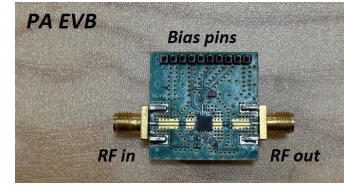


Fig. 4. Skyworks SE5004L-EK1 EVB used for PA characterization.

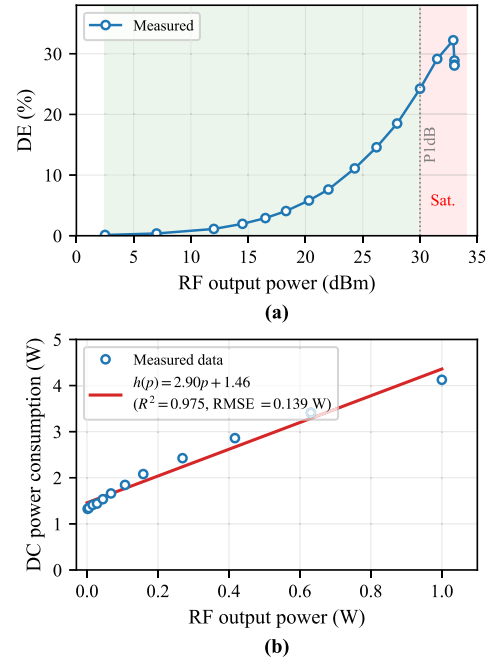


Fig. 5. PA characterization results. (a) Measured DE versus RF output power ( $V_{CC} = 5$  V). (b) DC power consumption versus RF output power.  $h(p) = 2.90p + 1.46$  is fit via least-squares regression ( $R^2 = 0.975$ ).

is biased at the rated supply voltage of  $V_{CC} = 5$  V. A CW signal is applied at the RF input, and for each input power level, the RF output power is recorded by spectrum analyzer while the DC power consumption is computed from the supply current measured at the EVB power supply ( $P_{DC} = V_{CC} \times I_{CC}$ ). Fig. 5(a) shows the measured DE across the full operating range.

The DE increases monotonically up to a peak of 32.2% near the compression point ( $P_{\text{out}} \approx 33$  dBm), beyond which the PA enters saturation, and the DE decreases. The PA characteristic is fit by a single affine function over the range  $P_{\text{out}} = 2.5$ –30 dBm (2 mW–1 W), corresponding to the linear region below the compression point. The saturation region is excluded because the RF output power compresses while the DC consumption continues to increase, offering no benefit to the optimizer. Over the fitting range, the measured DC consumption exhibits a nearly affine relationship with the RF output power, as shown in Fig. 5(b). Although a slight concavity is observed at low power levels (a typical characteristic of class-AB bias), the affine regression achieves  $R^2 = 0.975$  and RMSE = 0.14 W over the full fitting range. The relative error reaches approximately 10% at the lowest power level (2 mW) but decreases rapidly with increasing power. Since the affine model overestimates the DC consumption in this region,

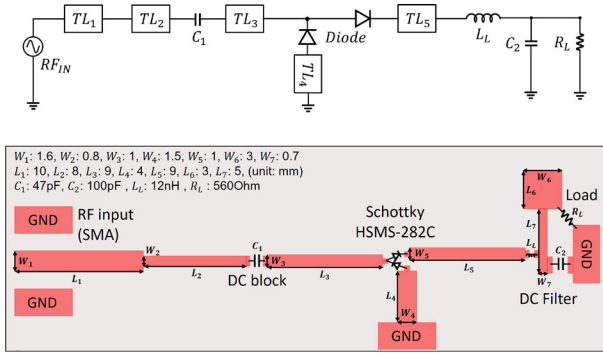


Fig. 6. Half-wave rectifier circuit: schematic (top) and layout (bottom).

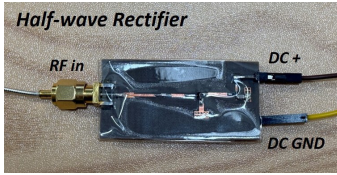


Fig. 7. Fabricated half-wave rectifier for 5.64 GHz.

the resulting  $\eta_{DC-DC}$  is a conservative estimate. The affine structure is specific to the class-AB PA used herein; other architectures (e.g., Doherty) would require recharacterization, though the framework remains applicable provided the PA model preserves convexity. The fit model is

$$h(p) = 2.90p + 1.46 \quad [\text{W}]. \quad (26)$$

This affine PA model simplifies the DC-to-DC SDP formulation in (18), where the total PA DC consumption reduces to a single linear constraint on  $S$ .

The rectifier model  $f(\cdot)$  is based on a simple half-wave rectifier designed and fabricated in-house for 5.64 GHz operation. Fig. 6 shows the circuit schematic and layout. The rectifier employs a Schottky diode (Avago HSMS-282C) with a microstrip matching network on a Taconic TLY-5A substrate (20 mil). The DC output filter consists of an inductor  $L_L = 12$  nH and a capacitor  $C_2 = 100$  pF, and the load resistance is optimized to  $R_L = 560 \Omega$ . The circuit is designed using Keysight ADS, targeting a peak PCE of approximately 51% at the design frequency. Fig. 7 shows the fabricated rectifier.

The rectifier PCE is characterized by sweeping the RF input power from a signal generator and measuring the DC output voltage across  $R_L$ , from which the DC output power is computed as  $P_{DC} = V_{DC}^2/R_L$ . Fig. 8(a) compares the ADS simulation and measured PCE. The measured peak PCE is 45.4% at an input power of 23 dBm.

The measured DC output power versus RF input power characteristic is shown in Fig. 8(b). A concave PWL function  $f(\cdot)$  is fit over the range 0–35 dBm (1–3162 mW), where the slopes remain monotonically decreasing, confirming the concavity required by the SDP formulation in (18). In the low-power linear region (the first segment), a linear regression is applied; in the higher power concave region, each segment directly connects consecutive measured data points without regression, enhancing the accuracy of the model. The complete segment parameters  $\{(a_k, b_k)\}$  are listed in Table V

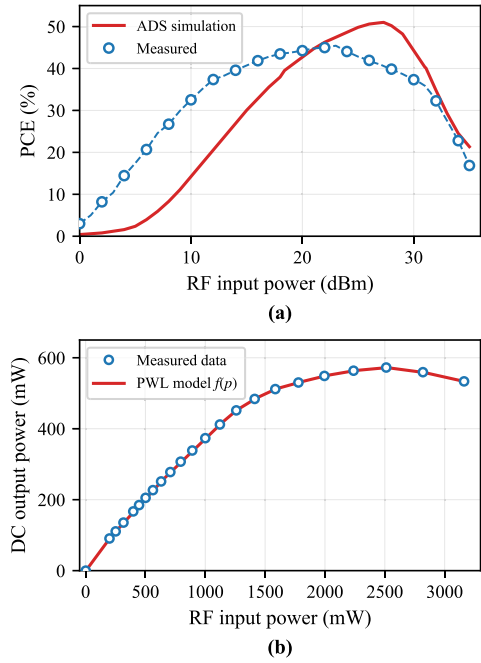


Fig. 8. Rectifier characterization results. (a) PCE versus RF input power: simulation and measurement. (b) DC output power versus RF input power. The concave PWL model  $f(p)$  is fit over the range 0–35 dBm.

TABLE II

SUMMARY OF KEY MODEL PARAMETERS AND OPERATING CONSTRAINTS

| Symbol                 | Description               | Value                       |
|------------------------|---------------------------|-----------------------------|
| $h(\cdot)$             | PA DC-consumption model   | $h(p) = \alpha p + \beta$ W |
| $\alpha$               | PA model slope            | 2.90                        |
| $\beta$                | PA model intercept        | 1.46 W                      |
| $f(\cdot)$             | Rectifier DC-output model | 12-segment PWL (Table V)    |
| $p_{TX,m}^{\max}$      | PA output limit           | 1 W (30 dBm)                |
| $p_{RX,n}^{\max}$      | Rectifier input limit     | 3162 mW (35 dBm)            |
| $P_{\text{rect,peak}}$ | Rectifier peak DC output  | 572 mW                      |

(see Appendix C). The key model parameters and operating constraints used throughout the simulation and experiment are summarized in Table II. The same ranges over which  $h(\cdot)$  and  $f(\cdot)$  are characterized are imposed as the operating constraints  $p_{TX,m}^{\max}$  and  $p_{RX,n}^{\max}$  in (18), so the device models and their valid ranges are identical across the simulation and experiment.

Three simulation scenarios are considered. In Scenario 1, the TXA and RXA sizes are swept jointly at a fixed distance to analyze the tradeoff between array size and end-to-end efficiency and to identify a suitable array size pair for the subsequent analyses. Scenario 2 uses the array configuration determined in Scenario 1 and evaluates the three optimization frameworks (RF-to-RF, RF-to-DC, and DC-to-DC) over varying propagation conditions, including distance and angular displacement. Scenario 3 fixes the propagation geometry and sweeps the DC power budget  $P_t^{\text{DC}}$  to examine how each framework responds to different transmit power levels. In all three scenarios, the same set of PA and rectifier PWL models is applied, and the results are compared in terms of both the  $\eta_{DC-DC}$  and the total received DC power  $P_{RX}^{\text{DC}}$ .

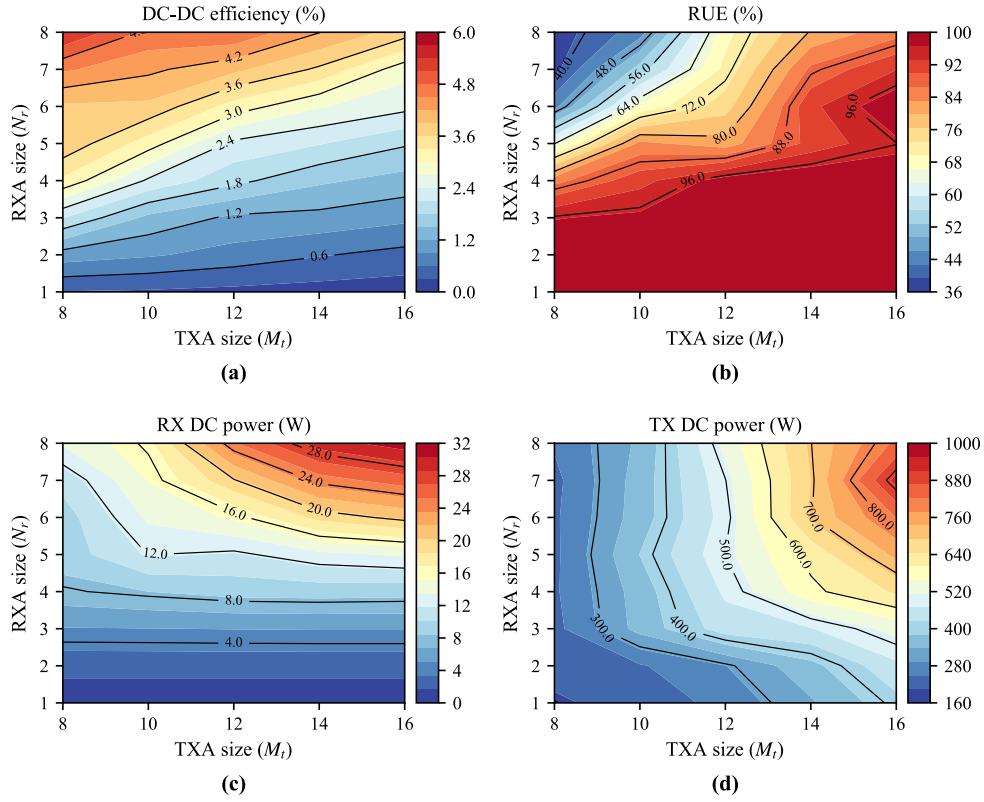


Fig. 9. Contour maps of (a) DC–DC efficiency, (b) RUE, (c) received DC power, and (d) TX DC power.  $d = 0.5$  m with  $P_t^{\text{DC}} = 1200$  W.

### B. Array Size Tradeoff Analysis

The proposed DC-to-DC optimization framework provides a system-level design tool for MIMO WPT, where the TXA and RXA sizes are fundamental design parameters that govern the tradeoff among efficiency, received power, and rectifier utilization. This section investigates these tradeoffs by sweeping the array sizes and identifies a suitable TXA–RXA pair for the analyses in Sections IV-C and IV-F.

The sweep covers  $M_t \in \{8, 10, 12, 14, 16\}$  for the TXA and  $N_r \in \{1, 2, \dots, 8\}$  for the RXA, yielding 40 combinations. Only the DC-to-DC optimization is applied. The DC power budget is set to  $P_t^{\text{DC}} = 1200$  W, which exceeds the maximum DC consumption of the largest array configuration ( $16 \times 16 = 256$  PAs, each consuming up to  $h(1.0) = 4.36$  W, totaling 1116 W), ensuring that the power budget does not artificially constrain any configuration. For the smallest  $8 \times 8$  TXA considered in this sweep, the diagonal aperture dimension is  $D = 8 \cdot (0.6\lambda) \cdot (2)^{1/2} = 0.361$  m. The corresponding reactive near-field boundary is  $0.62(D^3/\lambda)^{1/2} = 0.583$  m. Therefore,  $d = 0.5$  m lies within the near-field region even for the smallest TXA, and hence for all larger TXA configurations considered in Fig. 9.

To quantify the receiver-side utilization, we introduce the rectifier utilization efficiency (RUE), defined as [31]

$$\text{RUE} = \frac{\sum_{n=1}^N P_{\text{RX},n}^{\text{DC,port}}}{N \cdot P_{\text{rect,peak}}} \quad (27)$$

where  $P_{\text{rect,peak}}$  is the peak DC output of a single rectifier. While the DC-to-DC efficiency  $\eta_{\text{DC-DC}}$  measures the system-

level end-to-end performance (ratio of total received DC to total consumed DC), RUE captures how effectively each individual rectifier is utilized relative to its maximum capacity. These two metrics are complementary: a high  $\eta_{\text{DC-DC}}$  does not guarantee high RUE, and vice versa.

Fig. 9 presents the contour maps of four metrics as functions of  $M_t$  and  $N_r$ . The DC-to-DC efficiency [see Fig. 9(a)] increases with larger  $N_r$  and smaller  $M_t$ . This is because a larger TXA, while delivering more power to the RXA, consumes disproportionately more DC power at the PA stage, resulting in a net decrease in end-to-end efficiency. Conversely, the total received DC power [see Fig. 9(c)] increases with both  $M_t$  and  $N_r$  due to the larger combined aperture, revealing a clear tradeoff between efficiency and received power.

The RUE [see Fig. 9(b)] exhibits a distinct behavior: it remains close to 100% when  $N_r$  is small, but drops sharply when  $N_r$  is large and  $M_t$  is small. This occurs because a small TXA produces a broad beam with limited focusing capability. When such a beam focuses a large RXA, the received power is distributed thinly across many rectifier elements, causing each rectifier to operate far below its peak PCE. In contrast, a large TXA focuses the beam more effectively in the near field, delivering sufficient power to each rectifier even when the RXA is large, thereby maintaining high RUE. The TX DC power [see Fig. 9(d)] confirms the expected trend: larger arrays on both sides consume more DC power.

To navigate the tradeoff between DC-to-DC efficiency and received DC power, we employ a Pareto front analysis, as shown in Fig. 10. A design point is Pareto-optimal if no other configuration simultaneously achieves both higher effi-

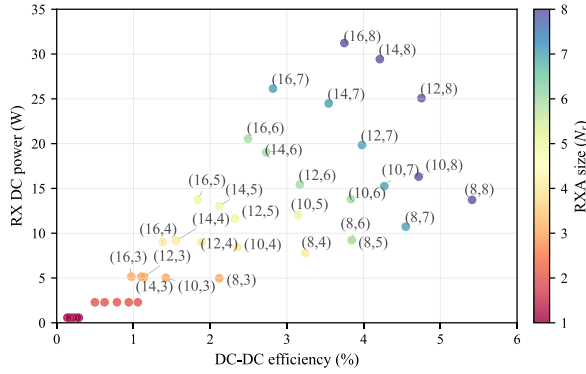


Fig. 10. DC-to-DC efficiency versus received DC power for all TXA-RXA combinations at  $d = 0.5$  m. Each marker is colored by  $N_r$ .

ciency and higher received power; improving one objective necessarily degrades the other. The Pareto-optimal configurations are  $(M_t, N_r) = (8, 8)$ ,  $(12, 8)$ ,  $(14, 8)$ , and  $(16, 8)$ , all sharing  $N_r = 8$ , indicating that maximizing the RXA size is always beneficial. The tradeoff is governed solely by the TXA size. Considering the balance between efficiency and received power across the Pareto front, we select  $(M_t, N_r) = (12, 8)$  as the operating configuration for the subsequent scenarios.<sup>7</sup>

### C. Efficiency Comparison Under Various Scenarios

This section compares the three optimizations as Fig. 11—RF-to-RF, RF-to-DC, and DC-to-DC—under varying propagation conditions using the array configuration  $(M_t, N_r) = (12, 8)$  selected in the previous subsection. For the  $12 \times 12$  TXA with  $M = 144$  PAs, the minimum DC consumption is  $M \cdot h(0) = 144 \times 1.46 = 210$  W, and the maximum at full power is  $M \cdot h(1.0) = 144 \times 4.36 = 628$  W. The DC power budget is set to  $P_t^{\text{DC}} = 400$  W, which is a reasonable intermediate value that ensures magnitude tapering across the array elements. For a fair comparison, the RF power budget  $P_t^{\text{RF}}$  of the PTE and TCE optimizations is set to the RF transmit power consumed by the DC-to-DC solution at each condition. Two propagation parameters are swept independently: the distance  $d$  from 0.5 to 3.0 m at broadside ( $\theta = 0^\circ$ ), and the azimuth angle  $\theta$  from  $0^\circ$  to  $60^\circ$  at  $d = 0.5$  m, as illustrated in Fig. 12.

Fig. 11(a) shows the three efficiency metrics as a function of distance. All metrics decrease monotonically with increasing distance due to the growing path loss. PTE shows the highest value trivially since it only accounts for the RF power transfer from the TXA to the RXA, without considering any nonlinearities. TCE is consistently lower than PTE because it additionally accounts for the rectifier PCE and the RX antenna radiation efficiency  $\eta_{\text{RX}}^{\text{rad}}$  in the rad-to-port path. The DC-to-DC efficiency, which further includes the PA DC consumption in the denominator, reaches 4.53% at its peak ( $d = 0.5$  m and  $\theta = 0^\circ$ ). Fig. 11(b) presents the SDP relaxation upper bound  $\bar{P}_{\text{DC}}$  and the recovered solution  $P_{\text{DC}}^*$  for the RF-to-DC and DC-to-DC frameworks. At short distances where

the channel exhibits high rank (rank = 4 for DC-to-DC at  $d = 0.5$  m), the SDR produces a higher rank  $S^*$ , resulting in a gap between  $\bar{P}_{\text{DC}}$  and  $P_{\text{DC}}^*$ . Nevertheless, the recovery ratio  $\rho_{\text{rec}} = P_{\text{DC}}^*/\bar{P}_{\text{DC}}$  remains above 97.5%, confirming the effectiveness of the SCA-based rank-one recovery. The RF-to-DC framework, which is free of the PA power constraint, which leads to low rank conditions, achieves near-perfect recovery ( $\rho_{\text{rec}} \geq 99.1\%$ ). As the distance increases beyond 1.5 m, the channel becomes increasingly rank-deficient; the SDP solution naturally converges to rank one, and all three methods yield nearly identical received DC power.

Fig. 11(c) and (d) presents the corresponding results for the azimuth angle sweep at  $d = 0.5$  m. All metrics degrade with increasing  $\theta$  due to the element gain roll-off. The bound-recovery gap narrows accordingly, with  $\rho_{\text{rec}}$  remaining above 97.1% across all angles.

Overall, both the distance and azimuth angle sweeps exhibit smooth and monotonic decreases in all efficiency metrics, consistent with the expected behavior. The SCA rank-one recovery achieves  $\rho_{\text{rec}} \geq 97.1\%$  across all tested conditions for the DC-to-DC framework, confirming that the SDR relaxation gap is negligible in practice.

The preceding analysis evaluates each framework by its own efficiency metric; however, to assess which optimization produces the best excitation vector in terms of actual end-to-end performance, all three must be compared under the same  $\eta_{\text{DC-DC}}$  criterion. Since the RF-to-RF and RF-to-DC frameworks do not impose PA constraints, their optimal excitation vectors may contain per-element RF powers exceeding the PA model max RF power (30 dBm). To ensure a fair comparison, PA clipping is applied—the magnitude of each element is limited to 1 W while the phase is preserved—and the clipped excitation is re-fed through the channel and an extended rectifier model to recompute the DC-to-DC efficiency.<sup>8</sup> Fig. 13 shows the resulting comparison. At  $d = 0.5$  m, the DC-to-DC optimization achieves  $\eta_{\text{DC-DC}} = 4.53\%$ , compared with 3.45% for RF-to-DC and 3.06% for RF-to-RF—representing relative improvements of 31.3% and 48.0%, respectively—confirming that jointly accounting for the PA and rectifier nonlinearities does yield a more efficient excitation. As the distance or angle increases, the received power decreases, and the nonlinear effects diminish, causing the three methods to converge beyond  $d \geq 1.5$  m or  $\theta \geq 40^\circ$ .

Notably, Fig. 11(b) shows that the received DC power of the DC-to-DC and RF-to-DC frameworks is nearly identical at short distances (18.1 versus 18.9 W at  $d = 0.5$  m). One might expect a tradeoff where the RF-to-DC framework, unconstrained by the PA, delivers substantially more received power at the cost of TX-side efficiency. In practice, however, the received power advantage of RF-to-DC is marginal, while the DC-to-DC framework achieves a 31.3% higher end-to-end efficiency by producing a PA-aware excitation that significantly reduces the TX DC consumption. This indicates

<sup>7</sup>For this configuration, the average computation times per instance are approximately 2 s (RF-to-RF), 2 min 15 s (RF-to-DC), and 4 min 37 s (DC-to-DC), measured in MATLAB with convex solvers.

<sup>8</sup>This post hoc clipping is not a rigorous reoptimization; a stricter approach would embed the PA and rectifier models into each framework. Since those frameworks are formulated without such models, the clipping-based re-evaluation provides the most reasonable basis for a unified comparison.

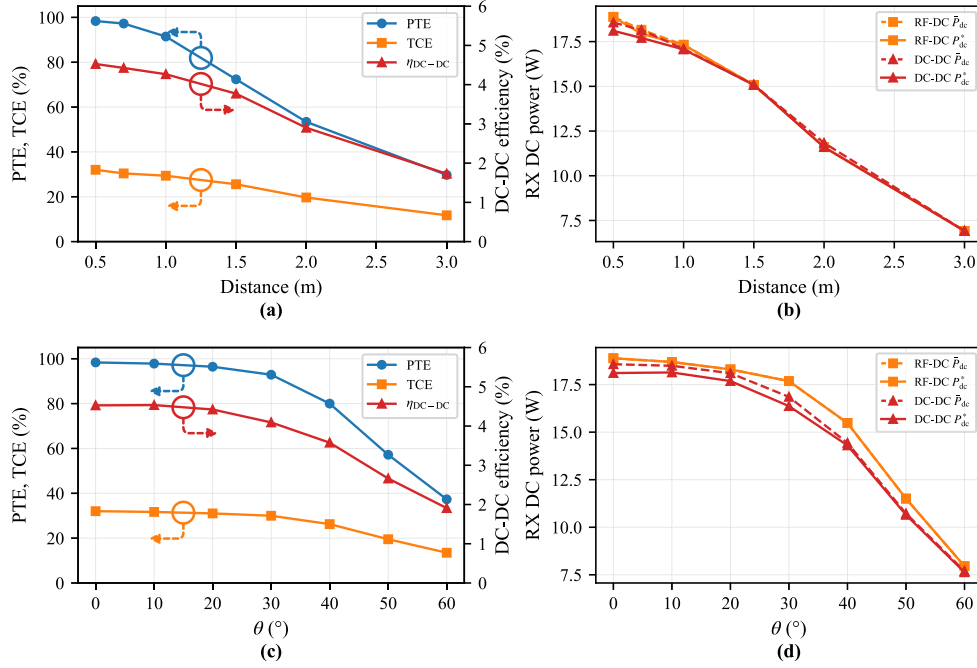


Fig. 11. Comparison of three optimization frameworks under varying propagation conditions with  $(M_t, N_r) = (12, 8)$  and  $P_t^{DC} = 400$  W. (a) PTE, TCE, and  $\eta_{DC-DC}$  versus distance. (b) SDP upper bound  $\bar{P}_{DC}$  and recovered  $P_{DC}^*$  versus distance. (c) Efficiency metrics versus azimuth angle at  $d = 0.5$  m. (d) SDP bound and recovered versus azimuth angle.

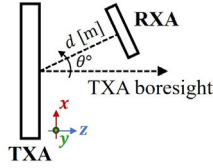


Fig. 12. Simulation geometry. The RXA is displaced by distance  $d$  along the boresight direction and rotated by azimuth angle  $\theta$ .

that the DC-to-DC optimization is not merely a different efficiency–power tradeoff point, but demonstrates a consistent system-level advantage in the near-field regime.

#### D. Stage-Level Efficiency Breakdown

To show how the end-to-end gain is distributed across the conversion chain, Table III decomposes  $\eta_{DC-DC}$  into its three stage efficiencies following (10) at the representative operating point  $(M_t, N_r) = (12, 8)$ ,  $d = 0.5$  m,  $\theta = 0^\circ$ , and  $P_t^{DC} = 400$  W. Each framework exhibits a clear efficiency peak precisely at the stage of its objective targets—RF-to-RF at the air-interface, RF-to-DC at the rectifier, and DC-to-DC at the PA. For the RF-to-RF and RF-to-DC frameworks, the stages absent from their objectives (marked by †) are evaluated by post hoc substitution into the  $h(\cdot)$  and  $f(\cdot)$ .

#### E. Efficiency Comparison Under Varying Power Budgets

This section investigates the effect of the DC power budget  $P_t^{DC}$  on the DC-to-DC optimization. From a system design perspective, when the size and geometry of the TXA and RXA are fixed, the DC power budget is a critical design

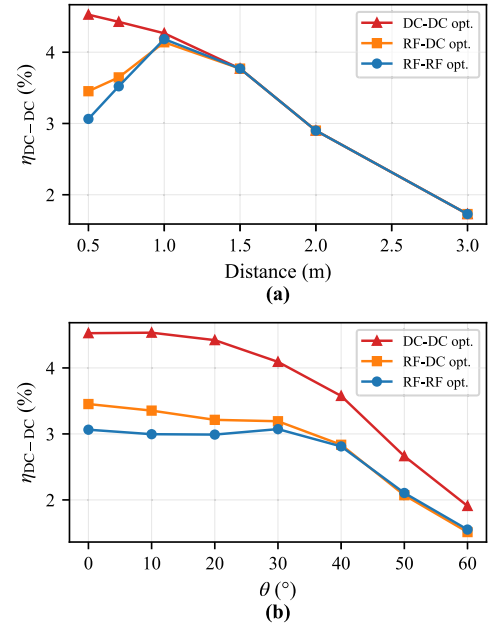


Fig. 13. Fair comparison of the three optimization frameworks evaluated under the same  $\eta_{DC-DC}$  metric. PA clipping is applied to the RF-RF and RF-DC excitation vectors prior to re-evaluation versus (a) distance and (b) azimuth angle.

parameter that governs the operating point of the system. In the configuration of  $(M_t, N_r) = (12, 8)$ ,  $d = 0.5$  m, and  $\theta = 0^\circ$ , the budget is swept over  $P_t^{DC} \in \{300, 400, 500, 600\}$  W; budgets below 300 W are infeasible as they cannot satisfy the minimum PA quiescent consumption of 210 W.

TABLE III

STAGE-LEVEL EFFICIENCY BREAKDOWN ( $M_t, N_r$ ) = (12, 8),  $d = 0.5$  m,  $\theta = 0^\circ$ , AND  $P_t^{\text{DC}} = 400$  W

| Framework | PA                    | Air                   | Rect.                 | End-to-end            |
|-----------|-----------------------|-----------------------|-----------------------|-----------------------|
|           | $\eta_{\text{DC-RF}}$ | $\eta_{\text{RF-RF}}$ | $\eta_{\text{RF-DC}}$ | $\eta_{\text{DC-DC}}$ |
| RF-to-RF  | 12.9% <sup>†</sup>    | 96.0%                 | 30.5% <sup>†</sup>    | 3.06%                 |
| RF-to-DC  | 11.7% <sup>†</sup>    | 89.2%                 | 40.8%                 | 3.45%                 |
| DC-to-DC  | 16.4%                 | 92.2%                 | 37.0%                 | 4.53%                 |

<sup>†</sup> Post-hoc value from substituting into  $h(\cdot)$  or  $f(\cdot)$  (not optimized).

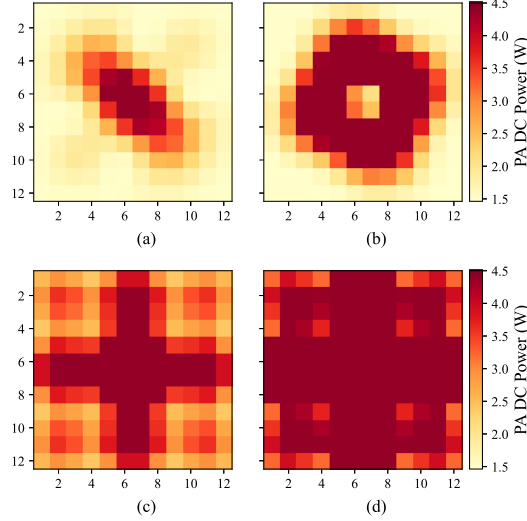


Fig. 14. Per-element PA DC power distribution of the  $12 \times 12$  TXA optimized by the DC-DC framework at  $d = 0.5$  m and  $\theta = 0^\circ$  for  $P_t^{\text{DC}} =$  (a) 300, (b) 400, (c) 500, and (d) 600 W.

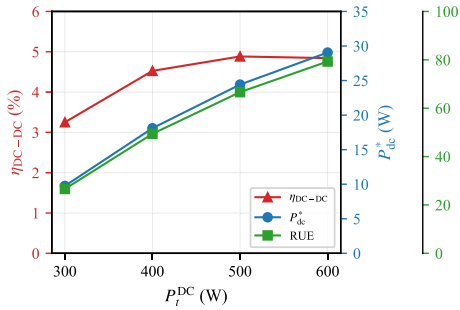


Fig. 15. DC-DC efficiency and received DC power  $P_{\text{DC}}^*$  versus DC power budget  $P_t^{\text{DC}}$  with  $(M_t, N_r) = (12, 8)$  at  $d = 0.5$  m and  $\theta = 0^\circ$ .

Fig. 14 shows the per-element PA DC power distribution optimized by the DC-to-DC framework across the  $12 \times 12$  TXA for each budget. As expected for the broadside configuration, the distributions exhibit symmetry.

Fig. 15 summarizes the corresponding  $\eta_{\text{DC-DC}}$  and  $P_{\text{DC}}^*$  as functions of  $P_t^{\text{DC}}$ . The received DC power increases monotonically from 9.8 W at 300 W to 29.1 W at 600 W. The efficiency peaks at  $P_t^{\text{DC}} = 500$  W ( $\eta_{\text{DC-DC}} = 4.88\%$ ) and slightly decreases at 600 W (4.84%). At 600 W, the mean per-PA DC consumption reaches 4.17 W out of the 4.36 W maximum, indicating that the TXA is operating near the PA saturation limit, while RUE remains at 79.3%, so the RXA still has headroom. The weak peak shape in this configuration

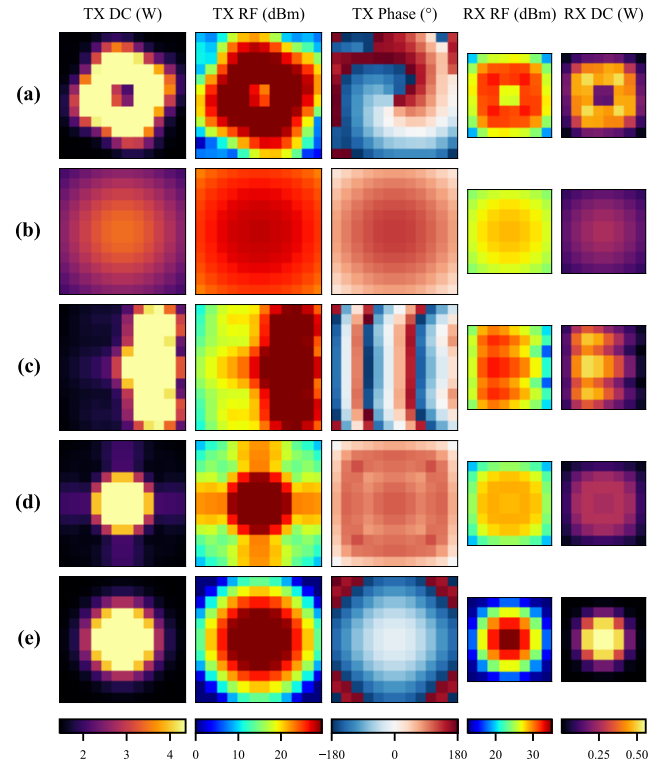


Fig. 16. Per-element excitation and received power maps for five cases. Columns from left to right: TX DC power (W), TX RF power (dBm), TX phase ( $^\circ$ ), RX RF power (dBm), and RX DC power (W). Each array is viewed from its own front face. (a) DC-DC,  $d = 0.5$  m, and  $\theta = 0^\circ$ . (b) DC-DC,  $d = 2.0$  m, and  $\theta = 0^\circ$ . (c) DC-DC,  $d = 0.5$  m, and  $\theta = 30^\circ$ . (d) RF-DC (clipped),  $d = 0.5$  m, and  $\theta = 0^\circ$ . (e) RF-RF (clipped),  $d = 0.5$  m, and  $\theta = 0^\circ$ .

is therefore dictated by the TX-side PA saturation rather than the RX-side rectifier saturation. Since this RX-side headroom is finite, it can be breached by enlarging the TXA to deliver more RF power, which pushes RUE toward 100%, as shown in Fig. 9(b) for increasing  $M_t$  at fixed  $N_r$ . However, this comes at the cost of a reduced  $\eta_{\text{DC-DC}}$  [see Fig. 9(a)]—an inherent tradeoff between RX utilization and end-to-end efficiency.

#### F. Excitation Pattern Analysis

Fig. 16 visualizes the per-element excitation patterns for five representative cases. Each row shows, from left to right, the TX PA DC power, TX radiated RF power, TX phase, RX radiated RF power, and RX DC power. Each array is depicted as viewed from its own front face. Rows (a)–(c) correspond to the DC-to-DC optimization under different propagation conditions, while rows (d) and (e) show the clipped RF-to-DC and RF-to-RF excitations at the same condition as (a) for direct comparison.

Fig. 16(a) and (b) illustrates the transition from near-field to far-field behavior. At  $d = 0.5$  m (a), the optimizer produces a nontrivial magnitude distribution with a complex phase pattern, and the RX DC power is broadly distributed across the  $8 \times 8$  RXA, confirming effective near-field focusing. At  $d = 2.0$  m (b), the channel approaches rank one, and the excitation converges toward a conventional far-field pattern with a narrow phase range and reduced received power. This

transition from near-field focusing to far-field beamforming is consistent with the expected qualitative behavior. Row (c) shows the  $\theta = 30^\circ$  case, where a phase gradient is clearly visible across the TXA columns, steering the beam off broadside. The resulting RX pattern exhibits a corresponding asymmetry.

Comparing Fig. 16(a), (d), and (e) at the same condition ( $d = 0.5$  m and  $\theta = 0^\circ$ ) reveals the fundamental differences among the three frameworks. The RF-to-DC excitation (d) concentrates power toward the center with a relatively smooth phase distribution, as the optimizer focuses on maximizing the rectifier output without PA awareness. The RF-to-RF excitation (e) shows a similarly centered magnitude pattern but with a nearly uniform phase, since PTE maximization does not benefit from phase diversity. In contrast, the DC-to-DC excitation (a) distributes power more broadly across the TXA, placing each PA at a favorable operating point while maintaining a complex phase pattern that effectively utilizes the full RXA aperture.

### G. Design Guidelines

The array-size analysis in Section IV-B guides the choice of the TXA and RXA sizes. Enlarging the RXA raises both the received DC power and the end-to-end efficiency, but it lowers the RUE when the TXA cannot focus enough power onto the larger aperture, leaving each rectifier underutilized. Enlarging the TXA restores focusing and increases the received power, yet it lowers the efficiency, since a larger array consumes more DC power at the PA stage.<sup>9</sup> In short, the RXA should be enlarged as far as the application allows, as long as the RUE stays acceptable. The TXA is then sized to keep the RUE high while meeting the target received power.

The propagation analysis in Section IV-C highlights the role of the operating regime. As the distance grows, the channel transitions from near-field focusing to far-field beamforming, and the three frameworks converge. The near-field excitation requires magnitude tapering and phase shaping, whereas the far-field excitation reduces to conventional beamforming. Unlike conventional approaches, the proposed framework provides a design solution across both regimes.

The power-budget analysis in Section IV-E shows that, for a fixed geometry, the DC power budget  $P_t^{\text{DC}}$  determines the operating point on the efficiency–power curve. Since the optimum budget varies with the scenario, and the DC-to-DC efficiency,  $P_{\text{DC}}^*$ , and the RUE all change considerably with  $P_t^{\text{DC}}$ , the budget should be determined by sweeping it and jointly considering these three metrics, yielding a system-optimized design.

## V. EXPERIMENTAL VALIDATION

### A. Measurement Setup

This section validates that the rank-one excitation vector obtained from the proposed DC-to-DC framework delivers the expected performance on real hardware. The overall measurement setup is shown in Fig. 17: a  $16 \times 16$  planar TXA

<sup>9</sup>The added DC consumption of a larger TXA can be mitigated by switching idle PAs to an OFF or reduced-bias state [26], [44].

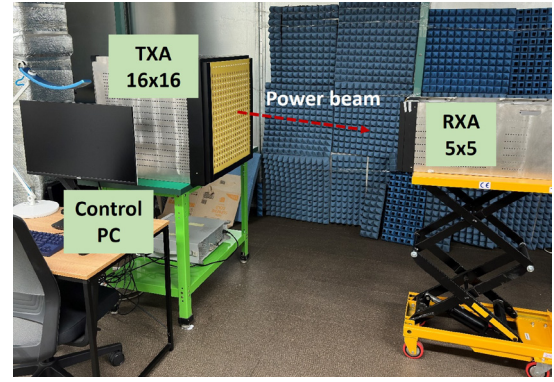


Fig. 17. Overall configuration in the laboratory free-space environment, with the  $16 \times 16$  TXA,  $5 \times 5$  RXA, and control PC.

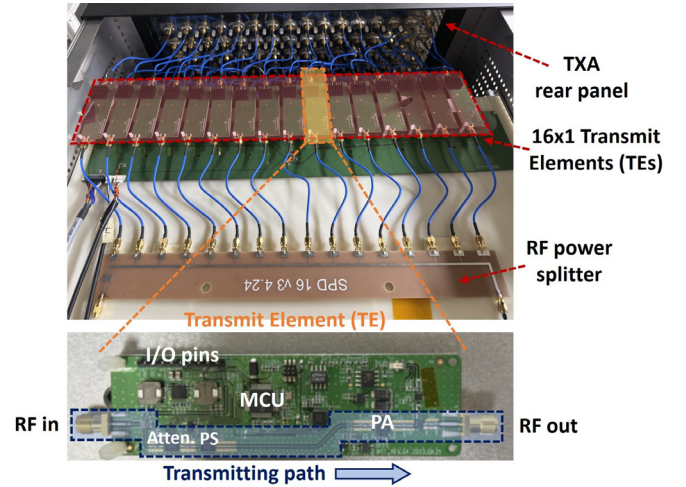


Fig. 18. Transmitter side. Close-up of a single TE showing the cascade of attenuator (Atten), PS, and PA on the PCB, integrated into the  $16 \times 16$  TXA.

operating at 5.64 GHz, a  $5 \times 5$  RXA whose elements use the half-wave rectifier characterized in Section IV-A, and a control PC that drives the TXA excitation and collects the RX DC readings. The system follows the architecture described in [40]. Since the Pareto-optimal  $(M_t, N_r) = (12, 8)$  selected in Section IV is not realizable on the fabricated array, the measurements employ the (16,5) configuration, which matches the fabricated prototype. The measurements are performed in a laboratory free-space environment.

Fig. 18 details the transmitter side. The close-up view shows a single TE, where an attenuator (Atten), a PS, and a PA are cascaded on the PCB.  $16 \times 1$  TEs form a 1-D subarray, which are then stacked to create the full  $16 \times 16$  TXA. Per-element control signals from the PC set the attenuation and phase of each TE so that the optimized excitation vector  $x_t^*$  is realized at the antenna ports.

Fig. 19 illustrates the receiver-side measurement scheme. The formulation assumes ideal DC combining at the RXA, but the prototype does not implement an actual DC summing network. As shown in Fig. 19(a), while the TXA continuously transmits the optimized beam, a single rectifier is manually moved from one RXA port to the next, and the remaining 24 ports are terminated by  $50\text{-}\Omega$  loads to preserve the array

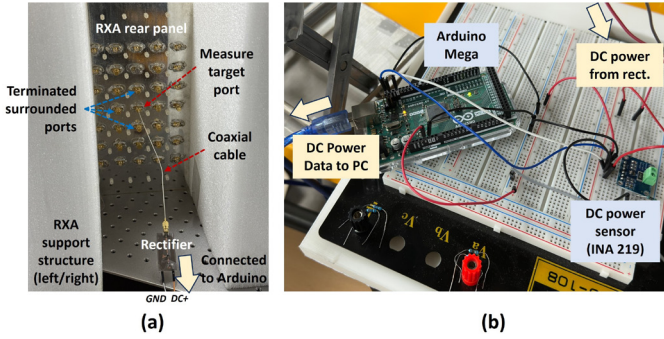


Fig. 19. Receiver-side measurement. (a) Single rectifier is sequentially placed at each of the 25 RXA ports while the remaining ports are 50- $\Omega$ -terminated, emulating ideal DC combining. (b) Rectifier DC output is monitored by an INA219 current-voltage sensor via an Arduino Mega that streams the readings to the PC.

loading conditions. The rectifier DC output [see Fig. 19(b)] is read by an INA219 current-voltage sensor through an Arduino Mega that streams the per-port reading to the PC. The 25 individual port readings are then summed in postprocessing to obtain the total received DC power, equivalent to the ideal DC combining assumed in the formulation.

### B. Measurement Procedure

For each measurement point, the rank-one excitation vector  $x_t^*$  obtained from the DC-to-DC optimization in Section III-D is applied directly to the TXA through the per-element control interface. Two sweeps are performed: the distance sweep varies  $d \in \{0.5, 0.7, 1.0, 1.5\}$  m at broadside ( $\theta = 0^\circ$ ), and the azimuth sweep varies  $\theta \in \{0^\circ, 20^\circ, 40^\circ, 60^\circ\}$  at  $d = 0.5$  m.

Since the assembled TXA does not permit direct per-element DC probing, the TX DC consumption is obtained by passing each element's measured RF port power through the PA model  $h(\cdot)$  in (26), whereas the RX DC power is measured directly via the per-port sweep of Fig. 19. The measurement-based models  $h(\cdot)$  and  $f(\cdot)$  characterized in Section IV-A are thus carried through both the simulation and the experiment without recharacterization, with  $f(\cdot)$  physically embodied by the fabricated rectifiers.

### C. Analysis of the (16, 5) Regime

The fabricated (16, 5) configuration differs from the previous (12, 8), so the result is expected to differ. The TXA is enlarged from 144 to 256 PAs, while the RXA is reduced from 64 to 25 rectifiers. This TX/RX size imbalance shifts the system into a different operating regime, which is analyzed next to determine the appropriate DC power budget.

Following the same procedure as Section IV-E, the DC power budget  $P_t^{\text{DC}}$  is swept from 400 to 800 W in 100-W increments, with the propagation parameters fixed at  $d = 0.5$  m and  $\theta = 0^\circ$ .<sup>10</sup> Fig. 20 shows the resulting  $\eta_{\text{DC-DC}}$ ,  $P_{\text{DC}}^*$ , and RUE. The received DC power rises from 2.9 W at 400 W to 13.5 W at 600 W, then saturates at 14.3 W near  $P_t^{\text{DC}} \approx 700$  W,

<sup>10</sup>The reference scenario ( $d = 0.5$  m and  $\theta = 0^\circ$ ) is retained across the configuration change for consistency throughout this article, since it supports a secure near-field condition for general scenarios.

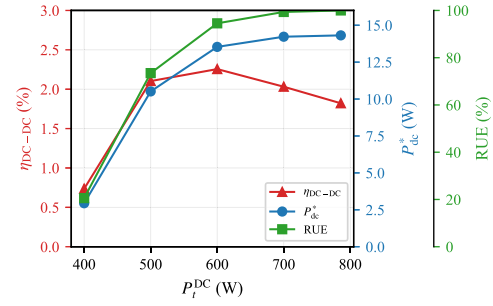


Fig. 20. DC-DC efficiency, received DC power, and RUE versus DC power budget for  $(M_t, N_r) = (16, 5)$  at  $d = 0.5$  m and  $\theta = 0^\circ$ .

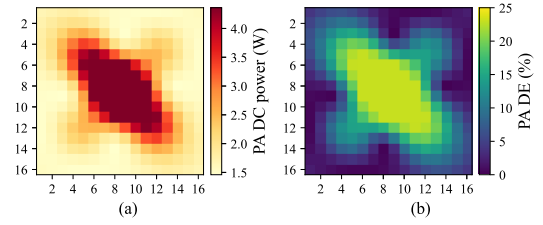


Fig. 21. Per-element maps of the  $16 \times 16$  TXA optimized by the DC-to-DC framework at  $P_t^{\text{DC}} = 600$  W,  $d = 0.5$  m, and  $\theta = 0^\circ$ . (a) PA DC power. (b) PA DE (mean = 13.0%).

at which point RUE reaches 99.4%. Beyond this point, further increases in  $P_t^{\text{DC}}$  produce negligible gain in  $P_{\text{DC}}^*$ , and the optimizer does not fully consume the budget: the actual TX DC consumption at an 800 W budget is 785.8 W. Consequently,  $\eta_{\text{DC-DC}}$  exhibits a pronounced peak at  $P_t^{\text{DC}} = 600$  W, reaching 2.26%, beyond which additional DC input is wasted as PA quiescent overhead. Unlike the (12, 8) case in Fig. 15, where the peak is only faintly visible because the PA saturation cap is reached before the RXA saturates, here the 25 rectifiers collectively saturate while the 256 PAs still operate below their limit, producing a clearer peak.

This peak,  $\eta_{\text{DC-DC}} = 2.26\%$ , is the maximum end-to-end efficiency achievable on the fabricated (16, 5) hardware.<sup>11</sup> Its structure is revealed in Fig. 21, which shows the per-element PA DC power [see Fig. 21(a)] and PA DE [see Fig. 21(b)] distributions at  $P_t^{\text{DC}} = 600$  W. The central elements are driven up to 4.36 W (near PA saturation) to form the near-field focus and reach DE above 20%, while the edge elements remain near the quiescent value of 1.46 W with DE below 5%, as total mean DE is 13.0%. Given the above, the measurements in the following subsection are performed at  $P_t^{\text{DC}} = 600$  W.

### D. Measurement Results

Fig. 22 compares the simulated and measured  $\eta_{\text{DC-DC}}$  for the DC-to-DC optimized excitation across both sweeps.

In the distance sweep [see Fig. 22(a)], both the simulation and the measurement exhibit a monotonic decrease with distance, with the measurement ranging from 2.15% at  $d = 0.5$  m to 1.85% at  $d = 1.5$  m. The measured values remain 5%–7%

<sup>11</sup>This value is limited by the prototype's commercial PA and simple rectifier, not by the framework itself; Section VI-B projects a peak DC-to-DC efficiency of 32.95% under SOTA device models.

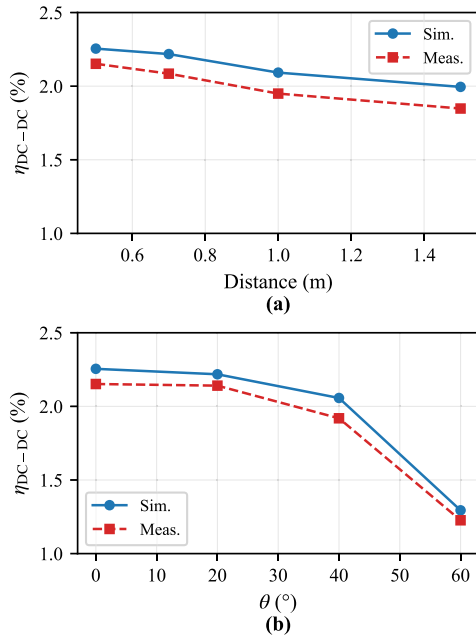


Fig. 22. DC-DC efficiency obtained from simulation and measurement for the  $16 \times 16$  TXA and  $5 \times 5$  RXA at  $P_t^{DC} = 600$  W. (a) Distance sweep at  $\theta = 0^\circ$ . (b) Azimuth angle sweep at  $d = 0.5$  m.

below the simulated ones across the entire range, which is within the various measurement nonidealities in the laboratory environment.

In the azimuth sweep [see Fig. 22(b)],  $\eta_{DC-DC}$  drops more steeply with steering angle, from 2.15% at broadside to 1.23% at  $\theta = 60^\circ$ . The measurement tracks the simulation with a comparable 3%–7% gap. Overall, the measured results confirm that the excitation produced by the proposed DC-to-DC framework delivers the expected end-to-end performance on the fabricated hardware, with the measured peak of 2.15% at the reference operating point within 5% of the framework-predicted 2.26%.

## VI. DISCUSSION

### A. Modeling Scope and Deployment

On the transmit side, only the PA consumption is modeled, for two reasons: it dominates the front-end power budget, and it is the only DC consumption that varies with the excitation. The attenuators, PSs, and digital control circuitry (e.g., SPI and MCU) draw small, *fixed power* independent of the excitation, so characterizing them would not affect the optimization; they are therefore omitted. On the receive side, the formulation assumes ideal lossless DC combining, which does not capture the output-voltage mismatch and DC-DC converter losses present in practical rectenna arrays.

The framework is derived for a free-space LoS channel, but the propagation environment enters only through the channel matrix  $\mathbf{G}$ . In the presence of clutter or backscatter, the same formulation applies once  $\mathbf{G}$  is replaced by the corresponding multipath or measured channel, with no change to the optimization itself.

TABLE IV

SIMULATED DC-TO-DC PERFORMANCE OF THE  $(M_t, N_r) = (12, 8)$  SYSTEM AT  $d = 0.5$  M AND  $\theta = 0^\circ$ : PROTOTYPE VERSUS SOTA

|                          | Prototype (Sec. IV) | SOTA (projected)  |
|--------------------------|---------------------|-------------------|
| PA                       | Commercial class-AB | GaN Doherty [45]  |
| Peak DE                  | 32.2%               | 69.8%             |
| Rectifier                | Half-wave Schottky  | Wideband GaN [46] |
| Peak PCE                 | 45.4%               | 71.0%             |
| $P_t^{DC}$               | 500 W               | 140 W             |
| Simulated $\eta_{DC-DC}$ | 4.88%               | 32.95%            |

### B. Projected Performance With State-of-the-Art Devices

The primary contributions of this work are the optimization framework and the accompanying design analysis; the absolute end-to-end efficiency is not itself a design target. For this reason, the experimental validation employs a commercial PA and a simple half-wave rectifier, which suffice to verify the framework but are not high-efficiency parts. Since the framework depends only on the measurement-based device models  $h(\cdot)$  and  $f(\cdot)$ , it is possible to project the efficiency attainable when SOTA devices are substituted. This section reports such a projection for a representative 5.8-GHz-band SOTA PA and rectifier. The device models are extracted by carefully digitizing the measured curves reported in the cited References, so the results are simulation-based projections rather than measured performance.

Following the same modeling procedure as Section IV-A, only the device data are replaced. The PA model adopts a high-efficiency GaN Doherty PA [45]; the affine  $h(p) = \alpha p + \beta$  is a least-squares fit over its high-efficiency power back-off range, with the slight plateau curvature absorbed as regression residual, thereby preserving the affine PA constraint of the formulation. The rectifier model adopts a wideband, high-PCE GaN rectifier [46], fit by the same concave PWL procedure. All other settings, such as the channel model and array size, remain identical.

Under the same scenario as Section IV ( $(M_t, N_r) = (12, 8)$ ,  $d = 0.5$  m,  $\theta = 0^\circ$ ), applying the proposed framework with the SOTA PA and rectifier yields a projected peak DC-to-DC efficiency of 32.95% at a DC power budget of  $P_t^{DC} = 140$  W. Table IV summarizes this projection against the corresponding Section IV result obtained with the prototype device models.

## VII. CONCLUSION AND FUTURE WORKS

This article presented an end-to-end DC-to-DC efficiency optimization framework for CW-based MIMO WPT systems that jointly accounts for PA and rectifier nonlinearities. Using an affine PA model and a concave PWL rectifier model extracted from measurements, the optimization was cast as an SDP under a DC power budget constraint, and an SCA procedure was developed to recover a feasible rank-one excitation vector from the relaxed solution. The SDP objective serves both as an upper bound on the achievable DC power and as a warm start for the SCA iterations, yielding a recovery ratio exceeding 97% across all tested conditions.

The RF-to-RF, RF-to-DC, and DC-to-DC formulations were systematically compared across various array-size, propagation, and power-budget scenarios. Jointly accounting for the PA and rectifier in the objective produces excitations that deliver 31% and 48% higher end-to-end efficiency than the RF-to-DC and RF-to-RF counterparts, respectively, at  $d = 0.5$  m in the near-field regime. Experimental validation on a fabricated  $16 \times 16$  TXA and  $5 \times 5$  rectenna confirmed that the measured DC-to-DC efficiency tracks the simulation across both distance and azimuth sweeps, verifying the practical applicability of the proposed framework for MIMO WPT system design.

To summarize, DC-to-DC efficiency is among the most important end-to-end metrics for WPT systems, but it has been addressed only indirectly in prior works. This framework takes it as the primary design objective, and the resulting upper bound on the achievable DC power can serve as a benchmark for future MIMO WPT designs.

Future work will include modeling realistic DC combining, with the development of low-loss DC-combining circuits at the device level, and pursuing real-time algorithms that approach the upper bound presented in this work.

## APPENDIX

### A. Proof of Affine Minorizer Properties

This appendix derives the affine minorizer  $\hat{q}_n(x_t; x_t^{(i)})$  used in the SCA subproblem (21). Define  $\varphi_n(x_t) = |g_n^H x_t|^2 / Z$ , which represents the received RF power at the  $n$ th rectifier. This function is convex in  $x_t$ , since it is a nonnegative scaling of the squared modulus of a linear function.

By the first-order condition for convex functions

$$\varphi_n(x_t) \geq \varphi_n(x_t^{(i)}) + \text{Re} \left( \nabla_{x_t} \varphi_n(x_t^{(i)})^H (x_t - x_t^{(i)}) \right) \quad (28)$$

for all  $x_t$ , where  $\nabla_{x_t} \triangleq 2 \partial / \partial x_t^*$  denotes the Wirtinger conjugate gradient, with  $x_t$  and  $x_t^*$  treated as independent variables. Applying this operator to  $\varphi_n$  gives

$$\nabla_{x_t} \varphi_n(x_t) = \frac{2}{Z} g_n (g_n^H x_t). \quad (29)$$

Substituting (29) into (28) and simplifying

$$\begin{aligned} \varphi_n(x_t) &\geq \frac{|g_n^H x_t^{(i)}|^2}{Z} + \frac{2}{Z} \text{Re} \left( (g_n^H x_t^{(i)})^* g_n^H (x_t - x_t^{(i)}) \right) \\ &= \frac{2}{Z} \text{Re} \left( (g_n^H x_t^{(i)})^* g_n^H x_t \right) - \frac{|g_n^H x_t^{(i)}|^2}{Z} \\ &= \hat{q}_n(x_t; x_t^{(i)}). \end{aligned} \quad (30)$$

This confirms the global lower bound property:  $\hat{q}_n(x_t; x_t^{(i)}) \leq p_{\text{RX},n}(x_t)$  for all  $x_t$ . The tangent point agreement follows directly by setting  $x_t = x_t^{(i)}$ :

$$\begin{aligned} \hat{q}_n(x_t^{(i)}; x_t^{(i)}) &= \frac{2 |g_n^H x_t^{(i)}|^2}{Z} - \frac{|g_n^H x_t^{(i)}|^2}{Z} \\ &= \frac{|g_n^H x_t^{(i)}|^2}{Z} = p_{\text{RX},n}(x_t^{(i)}). \end{aligned} \quad (31)$$

TABLE V

CONCAVE PWL PARAMETERS OF THE RECTIFIER MODEL  $f(\cdot)$ 

| $k$ | $P_{\text{rf}}$ range (dBm) | $P_{\text{rf}}$ range (mW) | $a_k$  | $b_k$ (mW) |
|-----|-----------------------------|----------------------------|--------|------------|
| 1   | [0, 23]                     | [1.0, 199.5]               | 0.460  | -1.20      |
| 2   | [23, 28]                    | [199.5, 631.0]             | 0.373  | 16.31      |
| 3   | [28, 30.5]                  | [631.0, 1122.0]            | 0.327  | 45.19      |
| 4   | [30.5, 31]                  | [1122.0, 1258.9]           | 0.291  | 86.01      |
| 5   | [31, 31.5]                  | [1258.9, 1412.5]           | 0.210  | 187.26     |
| 6   | [31.5, 32]                  | [1412.5, 1584.9]           | 0.161  | 256.73     |
| 7   | [32, 32.5]                  | [1584.9, 1778.3]           | 0.096  | 359.57     |
| 8   | [32.5, 33]                  | [1778.3, 1995.3]           | 0.086  | 378.13     |
| 9   | [33, 33.5]                  | [1995.3, 2238.7]           | 0.061  | 428.16     |
| 10  | [33.5, 34]                  | [2238.7, 2511.9]           | 0.033  | 490.09     |
| 11  | [34, 34.5]                  | [2511.9, 2818.4]           | -0.043 | 680.00     |
| 12  | [34.5, 35]                  | [2818.4, 3162.3]           | -0.075 | 771.79     |

Finally,  $\hat{q}_n(x_t; x_t^{(i)})$  is affine in  $x_t$  because it consists of  $\text{Re}(\cdot)$  applied to a linear function of  $x_t$  plus a constant.

### B. Convergence of the SCA Iterates

This appendix proves that Algorithm 1 produces a monotonically nondecreasing objective sequence that converges to a KKT stationary point of (19).

Let

$$F(x_t) = \sum_{n=1}^N f(p_{\text{RX},n}(x_t)) \quad (32)$$

be the original objective and

$$\tilde{F}(x_t; x_t^{(i)}) = \sum_{n=1}^N f(\hat{q}_n(x_t; x_t^{(i)})) \quad (33)$$

be the surrogate objective at iteration  $i$ . Define  $x_t^{(i+1)} = \arg \max \tilde{F}(x_t; x_t^{(i)})$  subject to the constraints in (21).

*Step 1 (Lower Bound):* Since  $\hat{q}_n(x_t; x_t^{(i)}) \leq p_{\text{RX},n}(x_t)$  for all  $x_t$  (see Appendix A) and  $f(\cdot)$  is nondecreasing over the valid operating range

$$F(x_t^{(i+1)}) \geq \tilde{F}(x_t^{(i+1)}; x_t^{(i)}). \quad (34)$$

*Step 2 (Optimality of Update):* Since  $x_t^{(i+1)}$  maximizes the surrogate and  $x_t^{(i)}$  is feasible

$$\tilde{F}(x_t^{(i+1)}; x_t^{(i)}) \geq \tilde{F}(x_t^{(i)}; x_t^{(i)}). \quad (35)$$

*Step 3 (Tangent Point Agreement):* By the tangent point property,  $\hat{q}_n(x_t^{(i)}; x_t^{(i)}) = p_{\text{RX},n}(x_t^{(i)})$ , so

$$\tilde{F}(x_t^{(i)}; x_t^{(i)}) = F(x_t^{(i)}). \quad (36)$$

Combining (34)–(36)

$$F(x_t^{(i+1)}) \geq \tilde{F}(x_t^{(i+1)}; x_t^{(i)}) \geq \tilde{F}(x_t^{(i)}; x_t^{(i)}) = F(x_t^{(i)}). \quad (37)$$

Thus  $\{F(x_t^{(i)})\}$  is monotonically nondecreasing. Since  $F(x_t) \leq \bar{P}_{\text{DC}}$  for all feasible  $x_t$  (the SDP upper bound), the sequence is bounded above and therefore converges. By standard SCA convergence theory [47], every limit point of  $\{x_t^{(i)}\}$  satisfies the KKT conditions of (19).

### C. Rectifier PWL Model Parameters

Table V lists the parameters of the concave PWL rectifier model  $f(\cdot)$  in (13), obtained as described in Section IV-A. Each segment  $k$  is given by  $f(P_{\text{rf}}) = a_k P_{\text{rf}} + b_k$ , where  $P_{\text{rf}}$  and  $f$  are in mW.

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